Numerical Simulation of Sinusoidal Fluctuated Pulsatile Laminar Flow Through Stenotic Artery

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ABSTRACT

A numerical investigation is carried out for laminar sinusoidal pulsating flow through a modeled arterial stenosis with a trapezoidal profile up to peak Reynolds number of 1000. Finite element based numerical technique is used to solve the fluid flow governing equations where the fluid is assumed to be viscous, incompressible and Newtonian. The effects of pulsation, stenosis severity, Reynolds number and Womersley number on the flow behavior are studied. The dynamic nature of pulsating flow disturbs the radial velocity distribution and thus generates recirculation zone in the post-stenotic region. The peak wall shear stress develops for 65% stenosis (by area) is 3, 2.2, and 1.3 times higher than that for 30%, 45%, and 55% stenosis, respectively. Peak wall shear stress and wall vorticity appear to intense at the throat of the stenosis. It is also observed that the peak wall vorticity seems to increase with the increase of stenosis size and Reynolds number. However, the peak values of instantaneous wall vorticity are not greatly affected by the variation of Womersley number.

Keywords: Stenosis, vorticity, wall shear stress, bio-fluid dynamics

1. INTRODUCTION

Investigation of the flow in a stenosed (constricted) geometry is of interest because of its significance in biomechanics especially in human vascular diseases. When too much cholesterol or high level of triglycerides (fatty substances) or both of them present in the blood, these fatty substances may begin to build as fatty streaks along the inside lining of the artery wall and causes the narrowing of the flow channel. Initially this streak grows very slowly. With course of time, as the hardening process and narrowing continues, the blood flow is disturbed. This thickening of stenotic artery was understood as an early process in the beginning of atherosclerosis which is the leading cause of human death in many countries. The haemodynamic behavior of the blood flow in arterial stenoses bears some important aspects due to engineering interest as well as feasible medical applications. In order to understand the effect of stenosis on blood flow through and beyond the constricted region of the artery, this has been the subject of much research both experimentally and numerically.

Numerical simulation of steady flow through axially symmetric rigid stenoses, with blood as a Newtonian fluid, have been reported by several investigators, among which are Deshpande et al. (1976), Lee (1990), Siegel et al. (1994), Reese and Thompson (1998). An integral interacting boundary layer theory for steady laminar flow in a asymmetrical bidimensional channel at high Reynolds number was presented by Largee (2007). They accounted the effect of asymmetry of the geometry in the ideal fluid pressure expression and observed that the effect is small but noticeable. Though these simulations were based on steady state situation, but actually blood flow through arteries is inherently unsteady due to the cyclic nature of the heart pump and Reynolds number can vary from 100 to 1000 for medium to large sized artery. Berger and Jou (2000) reviewed the modeling studies and experiments on steady and unsteady, two and three dimensional flows in arterial geometries most relevant in the context of atherosclerosis. The technique of large-eddy simulation (LES) has been applied to the study of pulsatile flow through a modeled arterial stenosis by Mittal et al. (2001). They used a simple stenosis model that consist of a one-sided 50% semicircular constriction in a planner channel. The inlet volume flux is varied sinusoidally in a manner similar to the laminar flow simulations of Tutty (1992). LES is used to compute the flow at a peak Reynolds number of 2000 and a Strouhal number of 0.024. Mahapatra et al. (2002) numerically solved unsteady Navier-Stokes equations by finite difference technique in staggered grid distribution for a flow through a channel with locally symmetric and asymmetric constrictions. For flow through symmetric constriction the centerline vertical velocity exhibited finite oscillation behind the constriction at high Reynolds...

number. Zendehbudi and Moayeri (1999) presented the numerical solutions for a physiological pulsatile flow as well as for an equivalent simple pulsatile flow, having the same stroke volume as the physiological flow. The analysis was restricted to laminar flow, Newtonian fluid and axisymmetric rigid stenosis. Liao et al. (2003) studied numerically the physiological turbulent flow fields in the neighborhoods stenosed arteries for Reynolds numbers from 1000 to 4000. The dimensionless diameter constriction ratios were allowed to vary from 0.375 to 0.6 for bell-shaped constrictions. The Womersley numbers were varied from 6 to 50. The solution procedure was based on the method of artificial compressibility with implicit LU-SGS and used a decoupled approach to solve the Reynolds-averaged Navier-Stokes equations and k-ε turbulence model equations.

Beside these, taking the non-Newtonian properties of the blood into consideration, there have been numerous studies. Tu and Deville (1996) simulated the blood flow through stenoses by incorporating the Herschel-Bulkley, Bingham and power-law fluids in the generalized incompressible Newtonian model. The geometry corresponded to a rigid circular tube with a partial occlusion. Ishikawa et al. (1998) used the bi-viscosity model as a constitutive equation for blood, and the flow was assumed to be periodic, incompressible and axisymmetric. They investigated the effect of pulsation and the rheological properties of blood. Also various mathematical models have been developed by a number of researchers (Jung et al., 2004; Chan et al., 2005 etc.) to simulate non-Newtonian blood flow through stenotic arteries.

Although the blood is known to be non-Newtonian in general, in the present study it is assumed to be Newtonian. This is because it is considered large arteries with radii of the order 1.0 mm, where the velocity and shear rate are high. The apparent viscosity is nearly a constant in arteries with relatively large diameters (~ 5 mm), and therefore the non-Newtonian effects can be neglected. Again the assumption of rigid boundary may not seriously affect the results since development of atherosclerosis in arteries causes a considerable reduction in the elastic properties of its wall.

The present study is concerned with laminar pulsatile flow in a tube with symmetric stenosis, which represents a simplified model of blood flow in stenosed arteries and to investigate the effects of pulsation, constriction ratio, Reynolds number and Womersley number on the flow property.

2. MATHEMATICAL MODELING

For axisymmetric flow of incompressible and Newtonian fluids with constant fluid properties, the continuity and Navier-Stokes equations in two-dimensional cylindrical co-ordinates (r,Z) can be written in the differential conservation form as follows:

Continuity equation:
\[
\frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial v_r}{\partial r} \right) + \frac{\partial v_z}{\partial z} = 0
\] (1)
r-direction momentum equation:
\[
\frac{\partial v_r}{\partial t} + v_r \frac{\partial v_r}{\partial r} + v_z \frac{\partial v_r}{\partial z} = -\frac{1}{\rho} \frac{\partial p}{\partial r} + \frac{\mu}{\rho} \left[ \frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial v_r}{\partial r} + \frac{\partial v_z}{\partial z} \right) \right]
\] (2)
Z-direction momentum equation:
\[
\frac{\partial v_z}{\partial t} + v_r \frac{\partial v_z}{\partial r} + v_z \frac{\partial v_z}{\partial z} = -\frac{1}{\rho} \frac{\partial p}{\partial z} + \frac{\mu}{\rho} \left[ \frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial v_r}{\partial r} + \frac{\partial v_z}{\partial z} \right) \right]
\] (3)

Here r and z are the radial and axial co-ordinates, respectively with the z-axis located along the axis of symmetry of the tube. The total velocity is defined by \( v_r \) and \( v_z \), the radial and axial components, respectively. The pressure, density and dynamic viscosity are denoted by \( p \), \( \rho \) and \( \mu \) respectively. Fig. 1 shows the physical solution domain of the present problem where \( \delta \) is the constriction radius (at the narrowest part of the stenosis) and \( R \) is the unconstricted radius.

The boundary conditions used in the present computations are:

- At the inlet: \( v_z = \frac{1}{A} \left[ Q + P \sin \left( 2\pi \frac{t}{T} \right) \right] \)
  \( v_r = 0 \).
- At the outlet: \( \frac{\partial v_r}{\partial z} = 0 \)
- At the centerline of the tube, axial symmetry condition.
- At wall, no-slip flow: \( v_r = v_z = 0 \)

Where \( A \) is the area of the unconstricted tube, \( Q \) is the mean flow rate, \( P \) is the pulsating amplitude, \( t \) is time and \( T \) is the time period of the pulsatile flow.

3. NUMERICAL SIMULATION

3.1 Computational Procedure

Present numerical procedure is based on the finite element method (FEM). Mixed finite-element formulation (Reddy and Gartling 1994) for pressure and velocity is used. The starting point for the development of this finite element model of equations (1-3) is their weak forms. Then the velocity and pressure will be approximated by their respective interpolation functions. The computational domain is subdivided into finite number of elements. The elements used are isoparametric triangular. Discretization is performed in such a way that the numbers of elements are higher near the stenosis and also on the post-stenotic region where higher gradients of the variable values are expected. Quadratic interpolation function for velocity and linear interpolation function for pressure are used. From the
particular input pulse allows a direct change to the
limiting high shear rate Newtonian viscosity. This
velocity, \(D\) is the blood vessel inlet diameter, and
validation is a 45% stenosis (by area) with a trapezoidal
from the center of the stenosis. The geometry used in the
stenosis; that is \(z = 0\) is the centerline of the
fluid. The ratio of
mean velocity.

\[
Re = \frac{\rho V_{\text{mean}} D \mu}{\mu}
\]

where \(V_{\text{mean}}\) is the time-averaged mean velocity, \(D\) is the blood vessel inlet diameter, and \(\mu\) is the
limiting high shear rate Newtonian viscosity. This
particular input pulse allows a direct change to the
Womersley number, \(Wo = R \left(2 \pi \rho / \mu T\right)^{1/2}\), the ratio of
transient inertial effects to viscous effects, without
altering the Reynolds number. The inlet pulse is
sinusoidal pulse with a mean Reynolds number of 575,
and the maximum and minimum Reynolds numbers are
930 and 230, respectively. The Womersley number for
this pulse is 7.75.

To analyze velocity variations of post-stenotic region,
the input centerline variations versus time are compared
in Fig. 4(a). The inlet boundary condition is assumed by
fully developed axial velocity profile. From the figure
it can be seen that the computed inlet centerline velocities
are similar throughout the pulse, expect near the peak of
the pulse to that experimentally obtained. This additional
acceleration in the experimental input pulse causes slight
discrepancies with the data. Again post stenotic velocity
profiles are used to validate the numerical computations
with experimental data as shown in Fig. 4(b). The
differences between the predictions and experimental
data are found to be great near the zenith of the pulse as
has been pointed out. However, the agreement is
generally well.

4. RESULTS AND DISCUSSIONS

In this section, sinusoidal fluctuated pulsatile laminar
flow through modeled stenosed artery will be discussed
in order to investigate the effect of stenosis size,
Reynolds number, Womersley number on the flow field.
To do so, velocity distribution, streamlines of the flow
field, wall vorticity, wall shear stress (WSS) under
different geometrical and physical configuration will be
high lightened. The flow waveform specified at the
present model inlet is similar to Ojha et al. (1989) except
that the experiment has a time-shift of 0.123 s (or phase
shift of about 128°) to that of present computation.

4.1 Radial Velocity Distribution in the Flow Field

The presence of a stenosis in an artery can greatly
influence on the flow field as shown in Fig. 5 for 55% stenosis,
\(Re = 575\) and \(Wo = 10\). The axial velocity
profiles for different positions at each time steps are
significantly different from a parabolic velocity profile
(Poiseuillean) for the Womersley number greater than one.
Figure 5(a) shows the velocity distribution just
upstream of the stenosis. At the beginning of the
pulsatile flow when \(t/T = 0\), the centerline velocity is
slightly higher than that for steady flow (2 times the
mean velocity). When \(t/T = 0.25\) that is for peak flow
rate, the centerline velocity is approximately 3 times of
mean flow velocity. Again at this time the instantaneous
velocity is always higher for all radial locations. At the
deceleration stage of the flow, when \(t/T = 0.5\), the
centerline velocity is 2.6 times the mean velocity of
flow. But region from the wall up to 0.3 times the radial
distance of the artery is found where velocity is always
lower than the steady velocity distribution. Beyond this
region velocity is always higher. At \(t/T = 0.75\), for all the
radial locations velocity is lower than the steady velocity
distribution due to the significant reduction in flow at
this time step. Here the center line velocity is 1.5 time
the mean velocity.

Figure 5(b) shows the velocity distribution at the throat
of the stenosis for different time steps. In this region, the
fluid accelerates and velocity reaches its maximum. The
velocity profile becomes flattened and reflects a

\[
\mu = \frac{\rho D}{2.6}
\]

The maximum velocity observed for these two
times are 2.75 and 4.25 times the mean velocity. At time $t/T = 0.5$, the centerline velocity is 3.1 times the mean one, whereas for $t/T = 0.75$, the velocity throughout the radius of the artery is lower compared to other time steps.

Beyond the stenosis region the flow slows down and there may be boundary layer separation as shown in Fig. 5(e). Due to sudden rise in area, the velocity distribution for all the time levels shows a region where flow velocity becomes approximately zero. This region is 0.3 times the radius of the artery. Beyond this region, velocity develops for all the time values.

Unsteady pulsed flow creates the disturbances in velocity distribution over the stenoses region. Velocity profile becomes very much flatter in the throat of the artery and downstream of the stenoses recirculation zone can be developed.

4.2 Streamlines, Wall Vorticity and WSS for Mean $Re = 575$, Wo = 10

Since the flow is pulsatile, the time-dependent flow field is more relevant for biomedical application. The instantaneous streamlines of the sinusoidally fluctuated flow show considerable variation through out the cycle as shown in Fig. 6 for 45% stenosis size. From Fig. 6 (a), at $t/T = 0$, just beginning of the pulsed flow, the streamlines run smoothly through the stenosis flow field with the creation of a vortex very close to the post stenotic region. The separation and reattachment points are very close to the separation point of the wall curve. At this instant, the Reynolds number is equal to the mean one. After this time, the flow accelerates to the peak flow rate, the attached vortex grow in size and became flatter as shown in Fig. 6 (b) for $t/T = 0.25$. When $t/T = 0.5$, the instantaneous Reynolds number equals the mean one during decelerated flow of the total flux, the vortex occupies more space in the distal area. When the flow rate reaches its zero net flux and relatively low velocities at $t/T = 0.75$, the remnants of these detached vortices occupy most of the constriction flow area, not only distal to the throat, but also proximal to the throat. After that, when $t/T$ advances to 1, the next cycle restarts and the flow field follows these repeated pattern.

Though the streamlines show the pictures of the flow field in more detail, the flow behavior can also be presented in more detail by wall vorticity distribution for different time steps as shown in Fig. 7(a). The wall vorticity is also varied during the cycle, being higher than the wall vorticity of the steady flows under the same mean Reynolds number in some parts of the cycle, and lower in other parts. For all the time steps, the wall vorticity is highest in the constriction area than any other positions throughout the channel. The peak wall vorticity is observed for $t/T = 0.25$ when the flow rate is peak. At time $t/T = 0$ and $t/T = 0.5$, the wall vorticity is also higher than the steady flow though the instantaneous Reynolds number is equal to mean one for these time levels.

Being the determining haemodynamic parameter in initiating the growth of atheroma, wall shear stress distribution along the axial direction are studied at different times during the cycle as shown in Fig. 7(b) for stenosis size of 55%. Maximum wall shear stress occurred in the stenosis throat, which is consistent with observations frequently reported on steady flows. The magnitude of wall shear stress is largest at $t/T = 0.25$ when flow is maximum in the cycle. The difference in upstream and downstream WSS in the post stenotic region indicates the creation of a vortex. The peak WSS for $t/T = 0.25$ is 2.25 and 3 times higher to that for $t/T = 0$ and 0.5, respectively. At $t/T = 0.75$, when net flux is zero shows a moderate rise in WSS at the stenosis throat.

4.3 Effects of the Reynolds Number

It is well known that the Reynolds number play a significant role on the flow field in the constricted tube for steady flow. The effect of the Reynolds number on the unsteady flow field will be discussed in the section. A constricted tube with 45% stenosis, Wo = 10 with mean $Re = 150$, 300 and 575 will be discussed.

The instantaneous streamlines for sinusoidally flow at $Re = 150$ and 300 are shown in Fig 8(a) and 8(b), respectively. Referring to the streamlines in Fig. 6, 8(a) and 8(b), at the point of $t/T = 0$, for $Re = 150$, the streamlines run smoothly through the constriction flow field with no significant creation of vortex. However, for $Re = 300$ and 575, there is a creation of a vortex in the streamlines. The size of the initial vortex is bigger for $Re = 575$ compared to $Re = 300$. At peak flow rate when $t/T = 0.25$, the attached vortex grows longer for $Re = 300$, and becomes shorter for $Re = 150$. After the peak flux, as the flow decelerates, the attached vortex still grows in size. Again for this time step ($t/T = 0.5$), the vortex size is small for $Re = 150$ compared to $Re = 300$ or $Re = 575$. At the time $t/T = 0.75$ when the flow rate reaches is zero net flux, the remnants of the detached vortices occupy the distal to the throat as well as the proximal to the throat. However, the shortest vortex is observed for $Re = 150$.

Since the magnitude of the peak wall vorticity near the stenosis at peak flow rate is higher than the ones at other time steps, only the comparison of instantaneous wall vorticity distributions at $t/T = 0.25$ is presented in Fig. 9 for brevity. The magnitude of maximum wall vorticity increases monotonically with the increase of Reynolds number. One more thing is observable that the location of the peak wall vorticity tends to shift slightly upstream as the Reynolds number increases. The peak wall vorticity for $Re = 575$ is 3 times higher than that for $Re = 300$. Again for $Re = 300$ and 575, the wall vorticity downstream the stenosis does not seem to regain its undisturbed upstream values as it does for $Re = 150$. This is due to the increase in size of the recirculation region for higher Reynolds number.

It can be concluded that the flow pattern can be greatly influenced by the variation of the Reynolds number. Higher Reynolds number can cause the peak wall vorticity to increase sharply.

4.4 Effect of Stenosis Size

It is obvious that the stenosis size has a great influence on the flow field in constricted tube. In this section, the variation of the flow with the variation of stenosis size will be discussed. The numerical results are compared.
The instantaneous streamlines for sinusoidal fluctuated flow at stenosis size of 30%, 55% and 65% are shown in Fig. 10(a), 10(b) and 10(c), respectively. Referring to the streamlines in Fig. 6, 10 (a), 10(b) and 10(c), at t/T = 0, for stenosis size of 30%, the streamlines run smoothly through the stenosis flow field. However, for 65% stenosis, there is a bigger vortex development compared to other stenoses. At the peak flow rate when t/T = 0.25, the attached vortex grows longer for 65% stenosis and becomes shorter for 30% stenosis. As the flow decelerates, the attached vortex continues to grow in size. When the flow rate reaches zero net flux at t/T = 0.75, the remnants of these detached vortices occupy distal to throat area. The shortest vortex is observed for 30% stenosis size. Unsteady flow field is more disturbed as the stenosis size increases.

Again, for the convenience of analysis, peak wall vorticity at peak flow rate is presented in Fig. 11. The value of maximum wall vorticity increases monotonically with increasing stenosis size. The value of maximum wall vorticity for stenosis size of 65% is approximately 3.25, 2.15, and 1.4 times higher than the corresponding values of vorticity when stenosis sizes are 30%, 45%, and 55%, respectively.

Figure 12 shows the variation of peak WSS for different stenosis severity at the time of maximum flow. The flow with the 65% stenosis is dominated by the wall shear stress especially in the stenosis position. For 30% stenosis, the peak WSS is 15 pa and the downstream WSS regain the value of upstream WSS very quickly due to small disturbances created by this stenosis which is not observable for higher stenosis size. The peak WSS for 65% stenosis is 3, 2.2, and 1.3 times higher than that developed for 30%, 45%, and 55% stenosis, respectively.

From these, it can be concluded that the severe stenosis size leads to a more complex flow field. The peak wall vorticity and WSS tend to increase with increasing stenosis size.

4.5 Effects of the Womersley Number

To investigate the effects of Womersley number, the details of the flow fields for different Womersley numbers are examined without varying the Reynolds number and the size of the stenosis. The Womersley numbers 5, 7.75, 10 and 12.5 are taken into consideration, with keeping the Reynolds number fixed to 575 and stenosis size of 45%.

Figure 13 shows the instantaneous wall vorticity distribution at peak upstream flow rate when t/T = 0.25 for the Womersley numbers of 5, 7.75, 10, and 12.5. It can be seen that the peak values of instantaneous wall vorticity are not greatly influenced by the variation of Womersley number. However, the wall vorticity downstream the stenosis for Wo = 12.5 recovers rapidly to the same level as that of the constriction upstream, while this is not a case for the Womersley numbers of 5, 7.75, and 10. For low Womersley number the recover process of wall vorticity is very slow.

The Womersley number can physically be interpreted as the ratio of unsteady to viscous force. The dynamic nature of the flow greatly depends on the frequency of the flow. The Womersley number does not greatly affect the maximum and mean wall vorticity distributions.

5. CONCLUSIONS

In this paper, a numerical simulation is presented to study the laminar flow through a modeled arterial stenosis. A simple axisymmetric model with a trapezoidal profile is chosen. The stenosis size is varied from 30% to 65% (by area). The flow at the artery inlet is taken as sinusoidal pulsated, and the peak Reynolds number was 1000. The effect of pulsation, stenosis size, Reynolds number and Womersley number are investigated by comparing the results of instantaneous streamlines, instantaneous radial velocity distribution, instantaneous wall vorticity, and wall shear stress as well.

From the numerical investigation of sinusoidal fluctuated flows, the following conclusions can be drawn:

i. The recirculation zone in the pulsating flow changes in size with time, due to the variation of instantaneous flow rate.

ii. The flow deceleration in the pulsating cycles tends to enlarge the recirculation zone.

iii. The recirculation zones always prefer to occur simultaneously both the proximal and the distal to the stenosis when the instant net flow rate approaches to zero.

iv. The flow disturbances become more severe for higher stenosis size. The peak wall vorticity for 65% stenosis is 3.25, 2.15, and 1.4 times higher than that for 30%, 45% and 55%, respectively. Similar impacts on other parameters are also found.

v. The variation of the Reynolds number can greatly influence the flow pattern. The peak wall vorticity is higher for higher Reynolds numbers than the ones for lower Reynolds numbers.

vi. Compared to other parameters, Womersley number does not have a significant influence on the peak values of wall vorticity.

REFERENCES


**Table 1** Grid independency test for mean Re = 575, Wo = 10.2

<table>
<thead>
<tr>
<th>Number of elements (degrees of freedom)</th>
<th>Peak Wall vorticity For</th>
<th>30% stenosis</th>
<th>45% stenosis</th>
<th>55% stenosis</th>
<th>65% stenosis</th>
</tr>
</thead>
<tbody>
<tr>
<td>7697 (37957)</td>
<td>100.5</td>
<td>148.78</td>
<td>225.2</td>
<td>307.32</td>
<td></td>
</tr>
<tr>
<td>8475 (41458)</td>
<td>106.0</td>
<td>151.8</td>
<td>230.1</td>
<td>314.1</td>
<td></td>
</tr>
<tr>
<td>10440 (50303)</td>
<td>106.0</td>
<td>152.3</td>
<td>238.78</td>
<td>316.25</td>
<td></td>
</tr>
<tr>
<td>11776 (56315)</td>
<td>106.0</td>
<td>152.4</td>
<td>239.55</td>
<td>318.68</td>
<td></td>
</tr>
<tr>
<td>14355 (67923)</td>
<td>106.0</td>
<td>152.4</td>
<td>239.5</td>
<td>318.64</td>
<td></td>
</tr>
<tr>
<td>19640 (91718)</td>
<td>106.0</td>
<td>152.4</td>
<td>239.5</td>
<td>318.64</td>
<td></td>
</tr>
</tbody>
</table>

**Fig. 1.** Geometry of the stenosis used in the simulations, where L = 1.5 mm and D = 5.0 mm. The normalized distance from the center of stenosis is given by $z' = Z/D$. On the right is the cross-sectional view of the model at the throat.
Fig. 2. Computational solution domain with finite element discretization of the present simulation

Fig. 3. The typical volumetric flow rate used in the simulation and that of Ojha et al. (1989)

Fig. 4. Comparison of the present numerical computation with that carried out by Ojha et al. (1989), (a) inlet centerline velocity profile and (b) centerline axial velocity at different post stenotic region.
Fig. 5. Instantaneous radial velocity distribution for 55% stenosis size with mean Re = 575, Wo = 10, (a) just upstream of the stenoses, (b) throat of the stenoses and (c) just downstream of the stenoses.

Fig. 6. Instantaneous streamlines for sinusoidal fluctuated flow when mean Re = 575, Wo = 10, 45% stenosis.
Fig. 7. Time dependent behavior of (a) wall vorticity of 45% stenosis and (b) wall shear stress of 55%, for Re = 575, Wo = 10.

Fig. 8. Instantaneous streamlines for sinusoidal fluctuated flow when (a) Re = 150 and (b) 300; 45% stenosis size, Wo = 10.

Fig. 9. Distribution of peak wall vorticity (at t/T=0.25) of 45% stenosis (Wo = 10) at various axial locations for different Reynolds number.
Fig. 10. Instantaneous streamlines for sinusoidal fluctuated flow when (a) 30% stenosis, (b) 55% stenosis, (c) 65% stenosis for mean Re = 575, Wo = 10.

Fig. 11. Comparison of peak wall vorticity distribution for different stenosis sizes at mean Re=575, Wo = 10.
Fig. 12. Distribution of peak WSS for different stenosis size at mean Re=575, Wo = 10.

Fig. 13. Comparison of peak wall vorticity of 45% stenosis for different Womersley number at mean Re = 575