Vortex Structure in the Wall Region of an Impinging Plane Jet

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ABSTRACT

The work presented here comes within a research program dealing with vortex detection in the impingement region of a planar jet. In this study, experiments have been performed for a submerged turbulent water slot jet impinging normally on a flat plate, and an emphasis was put on the flow field characteristics. For this purpose, particle image velocimetry (PIV) have been employed. A comprehensive fluid mechanical data includes instantaneous and mean flow field, variance of normal and cross velocity fluctuations have been presented. The present work is also concerned with the flow structure in the impingement region where the transfers (heat/mass) occur. An attempt has been made to understand the flow structure by employing the vortex detection criteria on the instantaneous velocity vector field. Accordingly, the PIV measurements were carried out for four different Reynolds numbers: 3000, 6000, 11000 and 16000, and at three different planes: a plane parallel to the impingement plate, transverse plane of the jet and a plane perpendicular to the jet. A method of filtration, based on proper orthogonal decomposition (POD) technique was applied first to the instantaneous velocity and filtered velocity database is then used for vortex detection. Further, the results about the size, shape, spatial distribution and energy content of the detected vortices have been provided.

Keywords: Planar water jet, Impingement, Vortex, POD, Coherence.

NOMENCLATURE

- $a(t)$: temporal coefficient
- $b$: Semi width of the nozzle (mm)
- $d_i$: Distance (mm)
- $e$: Nozzle width
- $f$: Frequency (Hz)
- $H$: Height of the jet (mm)
- $h_i$: Thickness of the impinging zone (mm)
- $I_w$, $I_v$: Turbulent intensity (%)
- $L$, $L_c$: Nozzle length (mm)
- $L_p$: Potential core length (mm)
- $M$: Number of spatial modes
- $Re$: Reynolds number
- $u, v$: Velocity components (m/s)
- $V_{max}$: Maximum velocity (m/s)
- $x, y$: Cartesian coordinates (mm)

Greek letters

- $\phi$: Spatial function or POD mode (m)
- $\lambda_2$: Criteria for vortex detection ($s^{-2}$)
- $\lambda_c$: Distance between vortices (mm)
- $\nu$: Kinetic viscosity (m²/s)

Superscripts

- $\bar{}$: Temporal average
- $'$: Fluctuation

Subscripts

- $max$: maximum

1. INTRODUCTION

Jet flows occur in many practical situations and are of great interest in many processes as well as in engineering applications. They are widely used for ambience separation in HVAC, fire safety (Pavageau and Gupta 2007), in food industry and in cooling of electronic components. Despite their wide range of applications, planar jets have not been studied as extensively as axisymmetric jets. Only a few authors have put forward this configuration and examined it in detail; Beltaos and Rajaratnam (1973), Gutmark et al. (1978) and Namer and Ötügen (1988). Planar jets...
exhibit different kind of instabilities. These instabilities originate either from streamlines with strong curvature in the impingement region or due to inflection in the transverse profile of the streamwise velocity component in the lateral mixing layers. Taking into account those instabilities vortices may occur. Our work has led to the identification of these flow structures in the impingement region. Previous works on impinging air jets were performed at the GEPEA laboratory; Maurel (2001), Beaubert (2002), Gupta (2005), Abide (2005), Pavageau and Loubière (2006). These works show the presence of vortices in the impingement region and their consequence on transport phenomena between the jet and the ambiance. Large Eddy Simulations (LES) (F. Beaubert and Viazzo 2003) have shown that it is in the impingement region that mass transfer across the jet stream preferentially occurs. A lot of studies deal with heat exchange at the impingement of jets. Gardon and Alkfarat (1965) studied this region in terms of heat transfer between the impinging jet and the impingement plate. Suetra et al. (1963 and 1965) explained the increase in heat transfer in the impinging region by the presence of vortices. Yokobori et al. (1983) showed experimentally, using visualization, roll vortices appearing in pairs of counter rotating rolls with their axis perpendicular to the plane of the jet. Pavageau and Loubière (2006) associated these rolls to Göertler vortices. However, Sakakibara et al. (2001) and Tsukokura et al. (2003) observed, experimentally and numerically using LES and Direct Numerical Simulation (DNS), that the twin vortices in the stagnation region are strongly related to the counter-rotating streamwise vortices observed in the braid region in mixing layers and across the symmetry plane of the jet. It has been also shown that they were characterized locally by a strong vortical intensity and noticeable energy content (Loubière and Pavageau 2008). From the foregoing discussion it is clear that, there were no studies which focused on the characterization of these vortices in terms of size, center positions, vortex intensity, eccentricity and statistical distribution except the work of Pavageau and Loubière (2006) for planar air jets. It is necessary to better understand the fashion in which the large-scale structures present in the impingement region of a jet form, evolve and contribute to transfer mechanisms. The aim of our work is to detect and characterize the roll cells vortices at the impingement. Further, the major studies reported in the literature deal with turbulent air jets. Planar water jets have received scant attention. Taking into account that the kinematic viscosity of water is smaller than air, at the same Reynolds number, it is easier to detect phenomena such as vortices. Phenomena can be observed at lower velocities making it possible to record signals with standard frequency bandwidths. Hence, it was thought desirable to undertake a systematic experimental study for confined planar submerged water slot jet impinging on a flat plate. PIV measurements have been performed in water for four different Reynolds numbers: 3000, 6000, 11000 and 16000. In order to detect vortices near the impingement, the instantaneous flow fields for different measurement planes were post processed first by employing POD decomposition. The analysis of the most energetic POD modes shows some specific zones with high level of energy. Later, the \( \lambda_3 \) criterion (Jeong and Hussain 1995) has been applied to expose vortices from the flow. They are then characterized in terms of size, shape, intensity, etc. Further, statistical analysis was also performed for all the recorded data.

2. Experimental Facility

2.1 Specifications

A schematic diagram of the experimental setup is shown in Fig. 1. The experimental facility consists of a rectangular tank with submerged rectangular slot nozzles at the bottom having the width \( e \) equal to 20 mm. The water pumped from another tank and discharged through this nozzle forms a planar jet flowing upward.

The jet impinges vertically on a flat plate fixed at a distance \( H = 200 \) mm from the nozzle (Fig. 2). The idea behind this is to set the geometrical aspect ratio (i.e. ratio of the height \( H \) of the jet and the nozzle width \( e \)) equal to \( H/e = 10 \), which is consistent with the earlier work reported from our laboratory. Further, at this ratio turbulent intensity at the jet axis is maximal comparing to other ratios (Maurel 2001).

![Fig. 1. Experimental setup](image1.png)

The ratio for the span of nozzle \( L = 400 \text{ mm} \) to the width of the nozzle \( e \) was set to \( L/e = 20 \) to preserve the bidimensionality of the flow.

![Fig. 2. Characteristic distances of the jet](image2.png)

The Reynolds numbers \( \text{Re}_{\text{base}} = V_{\text{max}} e / \nu \) were calculated using the exit velocities \( V_{\text{max}} \) at the nozzle, width of nozzle \( e \) and kinetic viscosity of water \( \nu \). The range of the Reynolds numbers has been chosen consistently with the works of Gupta (2005) and Yokobori et al. (1983). They mentioned that the Reynolds number strongly influences the mean and fluctuating characteristics of the jet when it is less than 6000.

So, in order to verify the consistency of their results in case of planar water jet, the study is performed for the wide range of Reynolds number. These Reynolds number cover three situations: under limit value...
Re=3000, the limit value Re=6000 and values greater than limit Re=11000 and Re=16000 which corresponds to flowrates of 5, 10, 15 and 20m³/h. The corresponding velocities at the exit of the nozzle respectively are: 0.2, 0.3, 0.55 and 0.8 m/s.

2.2 PIV Measurements

The PIV experiments were performed using a LaVision system for two different measurements planes of the jet: longitudinal and transverse plane. The schematic of the measurement arrangement of PIV is shown in Fig. 3.

![Fig. 3. Measurement planes considered for PIV technique: a) Transverse plane ; b) Longitudinal plane](image)

The laser source adopted was a double pulsed Nd-Yag laser that had power 125 mJ/pulse and produces laser beam of 532 nm wavelength. It was synchronized with the camera using a synchronizer. The laser excites polyamide tracer particles (diameter equal to 20µm) in the flow. A multiframe camera, with CCD sensor resolution of 1600 x 1200 pixels divided into small interrogations areas of 16 x 16 pixels, detects the light reflected by particles at two consecutives positions and instants. An adaptative algorithm based on cross-correlation technique permits to calculate the vector field associated to the displacement of the different particles in the field of view. To increase the number of vectors, we use overlapping areas (mostly 50%) in the two directions. The acquisition frequency of the camera is set to 15 Hz. The time duration of recorded flow is 60 seconds. The first configuration (Fig. 3a) is considered for characterization of the flow and the second one (Fig.3b) to examine the impingement region specifically.

3. Flow Characterization

Many authors reported interesting phenomena about the influence of Reynolds number on the development of the jet: expansion and velocity fluctuations. Tailland et al. (1967) have shown that for a range between 8500 and 38000, Reynolds number was not affecting the development of the jet. However, Namer and Ötügen (1988) have shown that the expansion rate of the jet is mainly affected by the Reynolds numbers between 1000 and 7000 and they proposed a limit value for the Reynolds number which was 6000. The same limit was also proposed by Maurel (2001), in study of planar air impinging jet with the important findings, that the influence of the Reynolds number still important in velocity fluctuations for Re ≥ 7000.

3.1 Flow Characterization at the Nozzle

Figure 4 below shows the velocity component (longitudinal and transverse) profiles at the nozzle exit for the different Reynolds number considered here: Fig 4a shows flat velocity profiles, which confirms that the flow is turbulent for all Reynolds numbers considered. Same observations were reported by Hussain and Clark (1977).

![Fig. 4. Velocity profiles at the nozzle (a) longitudinal-component (b) transverse-component](image)

Figure 4b shows profiles of transversal velocity component u at H/e = 10. From Figs. 4a and 4b it has been also observed that the profiles of mean longitudinal and transverse velocities seem not to be affected by the variation of Reynolds number, unlike turbulent intensities and Reynolds tensor i.e. I_u = \sqrt{\bar{u'^2}/V_{max}}, I_v = \sqrt{\bar{v'^2}/V_{max}} and I_{uv} = \bar{u'}v'/V_{max}^2 (Figs. 5 a-c). Figures 5a and 5b show the profiles of turbulent intensities I_u and I_v at the exit nozzle for each Reynolds number considered. The Figs. 5 a-c shows the important turbulent activities near the boundary of the nozzle which shows the starting of the mixing layers near the shear zone of the jet. The maximum of I_u (Fig. 5a) reaches 17% for Re=16000 and 8% for Re=3000, however, the maximum of I_v (Fig. 5b) didn’t exceed 6%.
3.2 Flow Structure

Figure 6 shows an example of the streamlines calculated from the mean velocity field measured in the transverse plane of the jet for Re=16000. It shows mainly three different regions in the jet whatever the Reynolds number considered.

The first region was observed nearly at \( y/e \approx 2 \) (Fig. 6) from the nozzle in the direction of mean flow, the second region where the jet starts expanding and the third region is the impingement region from where the streamlines change directions and become tighten. Here, authors would like to put emphasize on the recirculation on both sides of the jet where the streamlines are concentric.

These three regions can be further verified by plotting the evolution of centerline longitudinal velocity (Fig. 7). The first zone identified here is the potential core where the axial velocity is nearly \( v \approx 0.99 \times V_{\text{max}} \). The potential core length has been observed \( L_e = 3 \times e \) for \( \text{Re} \geq 6000 \) and \( L_e = 1.5 \times e \) for \( \text{Re} < 6000 \). According to literature, the potential core length was found between 3 and 5 times the nozzle width (Maurel 2005). It can be seen also that, the length of the potential core was affected for \( \text{Re} < 6000 \). This has also been observed in the past by Beltaos and Rajaratnam (1973), Rajaratnam (1976), Antonia et al. (1983), Lepicovsky (1986) and Maurel (2001).

The second zone identified is the developed region. Different empirical correlations were proposed in the literature to describe the profiles of velocity in this region.

Beltaos and Rajaratnam (1973) proposed a given correlation:

\[
\frac{V(y)}{V_{\text{max}}} = 2.5 \times \left( \frac{y}{H} \right)^{\frac{1}{2}}
\]

While, Maurel and Sollec (2001) and Maurel et al. (2004) proposed another correlation which gives better fit with our data:
Nevertheless, the empirical coefficients $C_1$ and $C_2$ are not the same. In the present work the constant considered were found equal to $C_1 = -2.4$ and $C_2 = 3.8$.

The third zone detected, is the impingement or the impact region. The centerline velocity decreases to zero at the impact. It is characterized by a significant lateral diffusion of momentum for the mean flow. Further, this region is of great interest as the significant transfers (heat/mass) appear in this region. Beltaos and Rajaratnam (1973) proposed a semi-analytical correlation for the decrease of centerline velocity in this region i.e.

\[
\frac{V(y)}{V_{\text{max}}} \sqrt{\frac{H}{e}} = C_1 \left(1 - \frac{y}{H}\right)^{\frac{2}{3}}
\]

with $C_1 = 5.5$

Later, Maurel (2005) proposed another correlation, which provides better fits with the present our experimental data:

\[
\frac{V(y)}{V_{\text{max}}} \sqrt{\frac{H}{e}} = C_4 \left(1 - \frac{y}{H}\right)
\]

with $C_4 = 15.5$

In the present study $C_4$ was set to 10.4.

The models proposed shows that the center line velocity is independent of Reynolds number.

The kinematic description of the impact region of the jet has not been the subject of many studies although significant transfers occur only in this region. The quantification and optimization of these transfers go through the understanding of mechanisms at their origin. Some works mostly in thermal heat exchange shows a link between the increase of heat transfer activity at the impingement and the longitudinal roll cells eddy structures formed at the impact of the jet (Tsubokura et al. 2003; Yokobori et al. 1983). We will especially focus in this region and on these structures in the following.

4. THE IMPACT ZONE OF THE JET

4.1 Thickness of the Impact Region

Gutmark et al. (1978) first estimated the thickness of the impact zone ($h_t$) for the planar air jet, which was about 15% of the total height of the jet (H). In the present work the thickness of the impact zone is determined from the longitudinal profiles of Reynolds stress $\overline{u'v'}$ at three different transverse ($x=0$, 2b and 3b) positions with different Reynolds number (Fig. 9). The changing in sign of Reynolds stress values for (from + to −) reflects the starting of impact region. From Figs. 9 it has been also observed that $h_t$ is slightly affected by the Reynolds number. Indeed, for $Re=3000$, the ratio $h_t/H = 10\%$ and it increases only to 13% for $Re=16000$ (Figs. 9). Pavageau and Gupta (2001), and Maurel and Solliec (2001) and Maurel et al. (2004) didn’t mention any influence of the Reynolds number in case of twin and simple planar air jet and reported a
4.2 Vortex at the Impingement Region of the Jet

PIV measurements give the global flow field of the jet. They also efficiently provide information about the associated eddy structures in the near-wall or impact region. Hence, it is quite possible to point out the influence of the impingement on the longitudinal and transverse mean flow. Four different Reynolds numbers were considered in order to study their influence on the size of the eddy structures at the impingement region. Yokobori et al. (1983) and Sakakibara et al. (1997) underlined the presence of the longitudinal roll cells counter rotating structures in the impinging zone. They specified that these structures were due to the fact that the impingement was at the level of the transition zone of a free jet; thus, they concluded without any strong argument that these structures disappear when $Re > 6000$, $ev = 5.0$, and in the case of $Re > 6000$ the distance $ev$ was found equal to $ev = 75.0$, Maurel and Solliec (2001), obtained a similar prediction, they found $ev = 0.75e$ for $Re = 13500$ and $He = 10$ for a planar air jet. However, this analysis is remaining based on instantaneous observations and didn’t confer to these results a general aspect.

To detect vortices at the impingement we considered PIV measurements on the mid-plane of the jet (Fig. 3b). Figure 10 shows the influence of Reynolds number on the distance between eddy structures of a same counter rotating pair of vortices ($\lambda_v$). It has been observed that for $Re < 6000$, $\lambda_v = 0.5e$ and in the case of $Re > 6000$ the distance $\lambda_v$ was found equal to $\lambda_v = 0.75 \times e$, Maurel and Solliec (2001), obtained a similar prediction, they found $\lambda_v = 0.8 \times e$ for $Re = 13500$ and $He = 10$ for a planar air jet. However, this analysis is remaining based on instantaneous observations and didn’t confer to these results a general aspect.

In most cases the flow structures are convected by the mean flow and couldn’t be detected from the direct analysis of velocity fields. In the present work, to extract them a method of filtration based on Proper Orthogonal Decomposition (POD) technique (Lumley et al. 1967) was applied first to the instantaneous velocity field. Filtration consists in removing from the fluctuating velocity fields the effects of perturbation on the flow (mainly due to laser reflexion, particle deposition, etc.). For that, the instantaneous velocity fields are first decomposed into M spatial functions (modes), noted $\phi^{(k)}(r)$, and temporal coefficient, noted $a^{(k)}(r)$:

$$a^{(k)}(r) = \sum_{k=1}^{M} a^{(k)}(r) \phi^{(k)}(r)$$

To exactly describe the velocity fields, 652 modes are necessary. A truncation to the 100 first most energetic modes (spatial and temporal) is done. The filtered velocity fields are later subjected to $\lambda_v$ criterion for the vortices center core detection.

4.3 Statistical Analysis

To detect vortices at the impingement, we considered PIV measurements on the plane $(y, z)$ of the jet (Fig. 3a). This plane is located at the center of the nozzle. Vortices occur at the impingement zone, so their maximum size will not exceed the thickness of the impinging zone $h_i$ evaluated in §3.1. Taking into account the variation of $h_i$ with Reynolds number, we consider a field size of $L \times 0.2H = 400 \times 40\text{mm}^2$.

For statistical analysis, we considered data from PIV measurement for total established flow duration of 30 seconds.

Typically, statistical analysis shows that the total number of vortices detected is around 5500 for each
Reynolds numbers under test: on average, this corresponds to twelve coherent structures per each instantaneous velocity field.

The characterization of vortices is made through the determination of the position of their center core, their sizes and shape. The $A_2$ criterion (Jeong and Hussain 1995) was used here for the detection of the center core of the vortex. This criterion relies on the basic assumption that a vortex core center is associated with the existence of a local pressure minimum. It has an interesting property which consists in discriminating swirling and shearing motion, what is not achievable by visualizing vorticity.

To characterize geometrically the detected vortices, we examined the spatial distribution of tangential component of velocity $V_t$ around the vortex center. It is here assumed that a vortex core is marked by an increase in tangential component of velocity with radial position inside the vortex, and by a decrease in tangential component of velocity with radial position outside. Subsequently, the size and shape of a detected structure is estimated by numerically finding the maxima of $V_t$ along 8 directions. These directions are defined by the angle they form with respect to the horizontal axis ($0^\circ, 180^\circ, 45^\circ, 225^\circ, 90^\circ, 270^\circ$ and $135^\circ, 315^\circ$).

Four diameters are estimated for each detected vortex $D_{\alpha}(\alpha = 0^\circ, 45^\circ, 90^\circ, 135^\circ)$ depending on the directions considered (Fig.12). The vortex radii defined as the distance to vortex centre from the point where, in the corresponding direction $\alpha$, $V_t$ reaches a maximum. From this, it is defined for each vortex:

- A mean diameter:
  \[ D_{\alpha} = \frac{1}{4} \sum_{\alpha=0^\circ,45^\circ,90^\circ,135^\circ} D_{\alpha} \]  
  \[ (6) \]
- An eccentricity:
  \[ E_c = \frac{\max(D_{\alpha})}{\min(D_{\alpha})} \quad \alpha = 0^\circ, 45^\circ, 90^\circ, 135^\circ \]  
  \[ (7) \]

![Fig. 12. (a) Tangential component velocity profile within the core of a vortex; (b) Radial directions considered for diameter estimation of the vortex](image)

The information below are stored for each vortex detected from series of instantaneous velocity fields:

- Number of the snapshot from which the structure was detected,
- Center core coordinates,
- Diameters $D_{\alpha}(\alpha = 0^\circ, 45^\circ, 90^\circ, 135^\circ)$ and eccentricity,
- Rotation direction (according to the sign of vorticity at center core of the detected vortex).

### Table 1 Statistic according to number of detected vortices and their rotation direction

<table>
<thead>
<tr>
<th>Re</th>
<th>Nbr. Of vortices</th>
<th>Clockwise</th>
<th>Anti-clockwise</th>
</tr>
</thead>
<tbody>
<tr>
<td>3000</td>
<td>5245</td>
<td>52%</td>
<td>48%</td>
</tr>
<tr>
<td>6000</td>
<td>5722</td>
<td>52%</td>
<td>48%</td>
</tr>
<tr>
<td>11000</td>
<td>5746</td>
<td>50%</td>
<td>50%</td>
</tr>
<tr>
<td>16000</td>
<td>5551</td>
<td>49%</td>
<td>51%</td>
</tr>
</tbody>
</table>

For each Reynolds number considered, the total vortices detected and fractions of their rotation direction are presented in the Table 1.

The figure below shows the distribution of vortices according to their range of size for each Reynolds number considered:

![Fig. 13. Statistical analysis on mean diameter of the detected vortices at the impinging zone](image)

Considering the results shown on Fig. 13, the Reynolds number has a slight influence on the number of the longitudinal roll cells occurring at the impingement. Noting also that Re=6000 seems to be a transitional value for the jet. Tsobukora et al. (2001) have predicted a similar behavior using LES and DNS simulations. A broad range of vortices coexist in the impingement region. Most of the detected vortices have their sizes between 5 and 30 mm (i.e. e/4 and 1.5e) with the maximum situated at nearly 20mm for all the Reynolds number considered.

![Fig. 14. Probability density function of eccentricity calculated for the detected vortices](image)
Here results show a similarity in tendency with the results of Loubière and Pavageau (2008). We notice the presence of two distinguish maximum at 1.9 and 3.5. Most of the vortices are characterized by an eccentricity range between 1.5 and 3.7. All these findings prove that the shape of the detected vortices is elliptical.

5. CONCLUSIONS

The present paper focuses on the development of planar vertical impinging water jet and the flow structure in the impingement region of such flow. The potential core length is found depending on the Reynolds number and reaches a maximum of $L_c = 3 \times e$. The evolution of the average velocity of the jet on its vertical axis is defined by the same law whatever the Reynolds number. The study was directed towards the impinging region. A characteristic height of this area was calculated. It is found slightly depending on the Reynolds number: for $Re=3000$, the ratio $h_i/H = 10\%$ and it increases only to 13% for $Re=16000$. Then, we focus on the vortex structure evolving in the impingement of the jet. A vortex eduding method developed in the laboratory was used to better understand the fashion in which the large-scale structures form, evolve and contribute to transfer mechanisms. The employed algorithm is based on $L_2$ criterion (Jeong and Hussain 1995). This criterion is used here to detect and locate the vortex core centers, the topological features of a structure being inferred from a local examination of the velocity field. It was found that:

- The Reynolds number of the flow has a slight influence on the number of vortices occurring at the impingement and their sizes.
- The shape of the detected vortices at the impingement is mainly elliptical.
- Vortex covering a wide range of sizes (from 5mm to 30mm) co-exists in this region.
- The fraction of vortices having clockwise rotation direction is close to the proportion of vortices having a counter clockwise rotation direction.

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