

Visco-Elastic MHD Free Convective Flow through Porous Media in Presence of Radiation and Chemical Reaction with Heat and Mass Transfer

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ABSTRACT

An analysis of visco-elastic free convective transient MHD flow over a vertical porous plate through porous media in presence of radiation and chemical reaction with heat and mass transfer is presented. A transverse variable suction velocity is applied on the porous plate. The equations governing the fluid flow, heat and mass transfer are solved by applying multiple perturbation technique. The expressions for transient velocity, temperature, species concentration and non-dimensional skin friction at the plate are obtained and the expressions for transient velocity and non-dimensional skin friction at the plate are illustrated graphically to observe the visco-elastic effect in combination of other flow parameters involved in the solution.

Keywords: MHD, Transient velocity, Chemical reaction, Radiation, Rarefaction parameter, Visco-elastic, skin friction, Grashof Number, Prandtl Number.

NOMENCLATURE

A	suction parameter.	\bar{T}_w	temperature of the plate.
B_0	uniform transverse magnetic field.	u, v	velocity components along x-and y-directions respectively.
\bar{C}	species concentration.	x, y	Cartesian coordinates.
C_p	specific heat at constant pressure.	Greek Letters	
\bar{C}_w	concentration at the plate surface.	β	volumetric co-efficient of expansion for heat transfer.
\bar{C}_∞	concentration in fluid far away from plate.	$\bar{\beta}_c$	volumetric co-efficient of expansion with species concentration.
D	chemical molecular diffusivity.	ε	perturbation parameter.
G_m	Grashof number for mass transfer.	η_0	limiting viscosity
G_r	Grashof number for heat transfer.	Θ	dimensionless temperature.
h	rarefaction parameter.	K	thermal conductivity of fluid.
K	porosity parameter.	k_e	mean absorption coefficient.
K_1	visco-elastic parameter.	P	density of fluid.
K_r	chemical reaction parameter.	ν	kinematic viscosity.
M	magnetic parameter.	v_0	mean suction velocity.
P_r	Prandtl number.	σ_s	Stefan-Boltzmann constant.
R	radiation parameter.	φ	dimensionless concentration.
S_c	Schmidt number.		
\bar{T}	fluid temperature.		
\bar{T}_∞	temperature in the free stream.		

1. INTRODUCTION

The study of visco-elastic fluid flows over vertical surfaces immersed in porous media in presence of magnetic field has attracted the researchers because of its application in geophysics, astrophysics, geohydrology, chemical engineering, biological

system, soil physics and filtration of solids from liquids. Also the studies of fluid flows through porous medium have become inevitable in the extraction of crude oil from the pores of rocks. The analysis of heat and mass transfer has attracted many researchers due to its application in geothermal and oil reservoir engineering studies. Sharma (2005) has studied the effect of fluctuating

thermal and mass diffusion on unsteady free convective flow past a vertical plate in slip flow regime. Singh *et al.* (2010a) have investigated heat transfer over stretching surface in porous media in presence of magnetic field. Singh *et al.* (2010b) have studied MHD oblique stagnation point flow towards a stretching sheet with heat transfer. Singh *et al.* (2010c) have studied the effect of thermal radiation and magnetic field on unsteady stretching permeable sheet in presence of free stream. Elbashbeshy *et al.* (2010) have analyzed heat transfer over an unsteady porous stretching surface embedded in a porous medium with variable heat flux with heat source or sink. Angirasa *et al.* (1997) have investigated heat and mass transfer by natural convection with opposing buoyancy effects in a fluid saturated porous medium. The dissipation effects on MHD non linear flow and heat transfer past a porous surface with prescribed heat flux have been investigated by Devi and Ganga (2010). Reddy and Reddy (2011) have studied the mass transfer and heat generation effects on MHD free convection flow past an inclined vertical surface in a porous medium.

The problems of heat and mass transfer in combination with chemical reaction are of great importance in many processes and have attracted the attention of many researchers. A reaction is said to be of the order n , if the reaction rate is proportional to the n -power of concentration. In particular, a reaction is said to be first-order, if the rate of reaction is directly proportional to concentration itself. In well mixed system, the reaction is heterogeneous if it takes place at an interface and homogeneous, if it takes place in solution. The effect of chemical reaction on free convection and heat transfer past an oscillating infinite vertical plate has been studied by Muthucumaraswamy and Meenakshisundaram (2006). Anjalidevi and Kandasamy (2000) have analyzed the effect of chemical reaction on MHD flow with heat and mass transfer past a semi-infinite plate. Choudhury and Jha (2008) have investigated the same on MHD micropolar fluid flow in slip flow regime. Al-Odat and Al-Azab (2007) have studied the influence of chemical reaction on transient MHD free convection over a moving vertical plate. Kandasamy *et al.* (2005) have investigated the influence of chemical reaction on MHD flow with heat and mass transfer over a vertical stretching sheet in presence of heat source and thermal stratification effect. Ahmed (2010) has analyzed the effect of chemical reaction on transient MHD free convective flow over a vertical plate in slip flow regime. Bala *et al.* (2012) have investigated the radiation effects on MHD flow past an exponentially accelerated isothermal vertical plate with uniform mass diffusion in the presence of heat source. Baoku *et al.* (2012) have analyzed the influence of thermal radiation on a transient MHD Couette flow through a porous medium. Basu *et al.* (2011) have studied the radiation and mass transfer effects on transient free convection flow of dissipative fluid past semi-infinite vertical plate with uniform heat and mass flux. Muthucumaraswamy and Chandrakala (2006) have

analyzed the radiation, heat and mass transfer effects on moving isothermal vertical plate in presence of chemical reaction. Rao *et al.* (2012) have found out the chemical effects on an unsteady MHD free convection fluid past a semi-infinite vertical plate embedded in a porous medium with heat absorption. El-Aziz (2009) has investigated the radiation effect on the flow and heat transfer over an unsteady stretching sheet. Sandeep *et al.* (2012) have investigated the effect of radiation chemical reaction on transient MHD free convective flow over a vertical plate through porous medium. Singh *et al.* (2010) have studied the effect of thermal radiation and magnetic field on unsteady stretching permeable sheet in presence of free stream velocity. Suneetha *et al.* (2010) have analyzed the radiation and mass transfer effects on MHD free convective dissipative fluid in the presence of heat source/sink.

The applications of the mechanisms of non-Newtonian fluid flows in modern technology and industries have attracted the researchers in a large scale. Keeping in view of the applications and the important roles played by the non-Newtonian fluid flow mechanisms in various manufacturing processes, authors like Kelly *et al.* (1999), Subhash *et al.* (2001), Sonth *et al.* (2002), Abel *et al.* (2007), Choudhury and Mahanta (2009), Choudhury and Dey (2010), Choudhury and Das (2012) etc. have analyzed some problems of physical interest in this field.

The objective of the present paper is to study the free convective transient MHD flow of non-Newtonian fluid characterized by Walters liquid (Model B') with heat and mass transfer in presence of radiation and chemical reaction past a vertical plate in a porous medium when a transverse variable suction velocity is applied on the porous plate and to observe the visco-elastic effects on the fluid flow field along with other flow parameters involved in the problem.

The constitutive equation for Walters liquid (Model B') is

$$\sigma^{ik} = -p g_{ik} + 2\eta_0 e^{ik} - 2K_0 e^{ik} \quad (1)$$

where σ^{ik} is the stress tensor, p is isotropic pressure, g_{ik} is the metric tensor of a fixed coordinate system x^i , v^i is the velocity vector, the contravariant form of e^{ik} is given by

$$e^{ik} = \frac{\partial e^{ik}}{\partial t} + v^m e^{ik}_{,m} - v^i_{,m} e^{im} - v^i_{,m} e^{mk} \quad (2)$$

It is the convected derivative of the deformation rate tensor e^{ik} defined by

$$2e^{ik} = v^i_{,k} + v^k_{,i} \quad (3)$$

Here η_0 is the limiting viscosity at the small rate of shear which is given by $\eta_0 = \int_0^\infty N(\tau) d\tau$ and $K_0 = \int_0^\infty \tau N(\tau) d\tau$ (4)

$N(\tau)$ being the relaxation spectrum as introduced by Walters (1960,1962). This idealized model is a valid approximation of Walters liquid (Model B') taking very short memories into account so that terms involving

$$\int_0^\infty \tau^n N(\tau) d\tau, \quad n \geq 2 \quad (5)$$

have been neglected.

2. MATHEMATICAL FORMULATION

A two dimensional unsteady free convective MHD flow of Walters liquid (Model B') with heat and mass transfer past a semi-infinite heated vertical porous plate immersed in a porous medium in presence of chemical reaction and radiation has been considered. The \bar{x} -axis is considered vertically upwards along the plate and \bar{y} -axis is taken normal to it. Let \bar{u} and \bar{v} be the fluid velocity along \bar{x} and \bar{y} directions respectively. A homogeneous chemical reaction of first order of constant rate \bar{K}_2 is assumed to exist between the diffusing species and the fluid. A transverse uniform magnetic field is applied normal to the plate.

We restrict our investigation to the following conditions:

- i) the induced magnetic field can be neglected as the transverse applied magnetic field and the magnetic Reynolds number are very small for metallic liquids and partially ionized fluids,
- ii) no electric field is present as there is no applied voltage,
- iii) Soret and Dufour effects are negligible as the concentration of diffusing species is very small in comparison with other chemical species,
- iv) temperature of the fluid is governed by energy equation involving radiative heat flux and species concentration is governed by concentration equation involving chemical reaction of first order.

With the above assumptions and the Boussinesq's approximation, the equations governing the fluid flow and heat and mass transfer are as follows:

equation of continuity:

$$\frac{\partial \bar{v}}{\partial \bar{y}} = 0 \quad (6)$$

Equation (6) shows that the suction velocity at the plate is either a constant or a function of time only. So, assuming the suction velocity to be oscillatory about a non-zero constant mean, one can write

$$\bar{v} = -v_0(1 + \varepsilon A e^{i\omega \bar{t}}) \quad (7)$$

Where v_0 is the mean suction velocity and ε, A are such that $\varepsilon A \ll 1$. The negative sign indicates that the suction velocity is directed towards the plate.

momentum equation:

$$\frac{\partial \bar{u}}{\partial \bar{t}} - \bar{v} \frac{\partial \bar{u}}{\partial \bar{y}} = \nu \frac{\partial^2 \bar{u}}{\partial \bar{y}^2} - \frac{K_0}{\rho} \left\{ \frac{\partial^3 \bar{u}}{\partial \bar{t} \partial \bar{y}^2} - \bar{v} \frac{\partial^3 \bar{u}}{\partial \bar{y}^3} \right\} + g\beta(\bar{T} - \bar{T}_\infty) + g\beta_c(\bar{C} - \bar{C}_\infty) - \frac{\nu \bar{u}}{\bar{K}} - \frac{\sigma B_0^2 \bar{u}}{\rho}$$

Or,

$$\frac{\partial \bar{u}}{\partial \bar{t}} - v_0(1 + \varepsilon A e^{i\omega \bar{t}}) \frac{\partial \bar{u}}{\partial \bar{y}} = \nu \frac{\partial^2 \bar{u}}{\partial \bar{y}^2} - \frac{K_0}{\rho} \left\{ \frac{\partial^3 \bar{u}}{\partial \bar{t} \partial \bar{y}^2} - v_0(1 + \varepsilon A e^{i\omega \bar{t}}) \frac{\partial^3 \bar{u}}{\partial \bar{y}^3} \right\} + g\beta(\bar{T} - \bar{T}_\infty) +$$

$$g\beta_c(\bar{C} - \bar{C}_\infty) - \frac{\nu \bar{u}}{\bar{K}} - \frac{\sigma B_0^2 \bar{u}}{\rho} \quad (8)$$

where $\nu = \frac{\eta_0}{\rho}$.

energy equation:

$$\frac{\partial \bar{T}}{\partial \bar{t}} - v_0(1 + \varepsilon A e^{i\omega \bar{t}}) \frac{\partial \bar{T}}{\partial \bar{y}} = -\frac{\kappa}{\rho C_p} \frac{\partial^2 \bar{T}}{\partial \bar{y}^2} - \frac{\partial \bar{q}_r}{\partial \bar{y}} \quad (9)$$

concentration equation:

$$\frac{\partial \bar{C}}{\partial \bar{t}} - v_0(1 + \varepsilon A e^{i\omega \bar{t}}) \frac{\partial \bar{C}}{\partial \bar{y}} = D \frac{\partial^2 \bar{C}}{\partial \bar{y}^2} - \bar{K}_2(\bar{C} - \bar{C}_\infty) \quad (10)$$

The boundary conditions are

$$\begin{aligned} \bar{y} = 0: \bar{u} &= \bar{L} \frac{\partial \bar{u}}{\partial \bar{y}}, \bar{T} = \bar{T}_w + \varepsilon(\bar{T}_w - \bar{T}_\infty) e^{i\omega \bar{t}}, \\ \bar{C} &= \bar{C}_w + \varepsilon(\bar{C}_w - \bar{C}_\infty) e^{i\omega \bar{t}} \\ \bar{y} \rightarrow \infty: \bar{u} &\rightarrow 0, \bar{T} \rightarrow \bar{T}_\infty, \bar{C} \rightarrow \bar{C}_\infty \end{aligned} \quad (11)$$

Using Rosseland approximation, which is valid for optically thick fluids, we get that

$$\bar{q}_r = -\frac{4\sigma_s}{3k_e} \frac{\partial \bar{T}^4}{\partial \bar{y}} \quad \text{where } \sigma_s \text{ is the Stefan Boltzmann constant and } k_e \text{ is the mean absorption coefficient.}$$

Expanding \bar{T}^4 into the Taylor series about \bar{T}_∞ which after neglecting higher order terms takes the form

$$\bar{T}^4 \cong 4\bar{T}_\infty^3 \bar{T} - 3\bar{T}_\infty^4 \quad (12)$$

On introducing the non-dimensional quantities

$$\begin{aligned} y &= \frac{v_0 \bar{y}}{\nu}, u = \frac{\bar{u}}{v_0}, t = \frac{\bar{t} v_0^2}{4\nu}, \omega = \frac{4\omega \nu}{v_0^2}, \\ P_r &= \frac{\mu C_p}{\kappa}, \theta = \frac{\bar{T} - \bar{T}_\infty}{\bar{T}_w - \bar{T}_\infty}, \phi = \frac{\bar{C} - \bar{C}_\infty}{\bar{C}_w - \bar{C}_\infty}, \\ G_r &= \frac{\nu g \beta (\bar{T}_w - \bar{T}_\infty)}{v_0^3}, G_m = \frac{\nu g \beta_c (\bar{C}_w - \bar{C}_\infty)}{v_0^3}, M = \frac{\sigma B_0^2 \nu}{\rho v_0^2}, \\ S_c &= \frac{\nu}{D}, h = \frac{v_0 \bar{L}}{\nu}, K_r = \frac{\nu \bar{K}_2}{v_0^2}, K = \frac{\bar{K} v_0^2}{\nu^2}, \\ R &= \frac{\kappa k_e}{4\sigma_s \bar{T}_\infty^3} \end{aligned} \quad (13)$$

Equations (8) to (10) and the boundary conditions (11) become

$$\begin{aligned} \frac{1}{4} \frac{\partial u}{\partial t} - (1 + \varepsilon A e^{i\omega t}) \frac{\partial u}{\partial y} &= \frac{\partial^2 u}{\partial y^2} - K_1 \left\{ \frac{1}{4} \frac{\partial^3 u}{\partial t \partial y^2} - \right. \\ &\left. (1 + \varepsilon A e^{i\omega t}) \frac{\partial^3 u}{\partial y^3} \right\} + G_r \theta + G_m \phi - Mu - \frac{u}{K} \end{aligned} \quad (14)$$

where $K_1 = \frac{K_0 v_0^2}{\rho \nu^2} \cdot \frac{1}{4}$.

$$\frac{\partial \theta}{\partial t} - (1 + \varepsilon A e^{i\omega t}) \frac{\partial \theta}{\partial y} = \frac{1}{P_r} \left(1 + \frac{4}{3R} \right) \frac{\partial^2 \theta}{\partial y^2} \quad (15)$$

$$\frac{1}{4} \frac{\partial \phi}{\partial t} - (1 + \varepsilon A e^{i\omega t}) \frac{\partial \phi}{\partial y} = \frac{1}{S_c} \frac{\partial^2 \phi}{\partial y^2} - K_r \phi \quad (16)$$

The modified boundary conditions are

$$\begin{aligned} y=0: u &= h \frac{\partial u}{\partial y}, \theta = 1 + \varepsilon e^{i\omega t}, \phi = 1 + \varepsilon e^{i\omega t} \\ y \rightarrow \infty: u &\rightarrow 0, \theta \rightarrow 0, \phi \rightarrow 0 \end{aligned} \quad (17)$$

For $\varepsilon \ll 1$, introducing the perturbation scheme

$$f(y, t) = f_0(y) + \varepsilon e^{i\omega t} f_1(y) + o(\varepsilon^2) \quad (18)$$

where f represents u, θ and ϕ in Eqs. (14) to (16) and comparing the coefficients of various powers of ε and neglecting those of second and higher powers of ε we get the following equations.

2.1. Zeroth-Order Equations

$$K_1 \frac{d^3 u_0}{dy^3} + \frac{d^2 u_0}{dy^2} + \frac{du_0}{dy} - \left(M + \frac{1}{K}\right) u_0 = -G_r \theta_0 - G_m \phi_0 \quad (19)$$

$$\frac{d^2 \theta_0}{dy^2} + NP_r \frac{d\theta_0}{dy} = 0 \quad (20)$$

$$\frac{d^2 \phi_0}{dy^2} + S_c \frac{d\phi_0}{dy} - Kr S_c \phi_0 = 0 \quad (21)$$

$$\text{where } = \frac{1}{1 + \frac{4}{3R}}.$$

2.2. First-Order Equations

$$K_1 \frac{d^3 u_1}{dy^3} + \left(1 - \frac{i\omega K_1}{4}\right) \frac{d^2 u_1}{dy^2} + \frac{du_1}{dy} - \left(M + \frac{1}{K} + \frac{i\omega}{4}\right) u_1 = -G_r \theta_1 - G_m \phi_1 - A \frac{du_0}{dy} - K_1 A \frac{d^3 u_0}{dy^3} \quad (22)$$

$$\frac{d^2 \theta_1}{dy^2} + NP_r \frac{d\theta_1}{dy} - \frac{i\omega P_r N}{4} \theta_1 = -ANP_r \frac{d\theta_0}{dy} \quad (23)$$

$$\frac{d^2 \phi_1}{dy^2} + S_c \frac{d\phi_1}{dy} - S_c \left(\frac{i\omega}{4} + Kr\right) \phi_1 = -A \frac{d\phi_0}{dy} \quad (24)$$

The corresponding boundary conditions are

$$y = 0: u_0 = h \frac{du_0}{dy}, u_1 = h \frac{du_1}{dy}, \theta_0 = 1, \theta_1 = 1, \phi_0 = 1, \phi_1 = 1$$

$$y \rightarrow \infty: u_0 \rightarrow 0, u_1 \rightarrow 0, \theta_0 \rightarrow 0, \theta_1 \rightarrow 0, \phi_0 \rightarrow 0, \phi_1 \rightarrow 0 \quad (25)$$

To solve Eqs. (19) and (22) we apply another perturbation scheme for $K_1 \ll 1$ as

$$u_0 = u_{00} + K_1 u_{01} + o(K_1^2)$$

$$u_1 = u_{10} + K_1 u_{11} + o(K_1^2) \quad (26)$$

and we get the following equations.

Zeroth- order equations:

$$\frac{d^2 u_{00}}{dy^2} + \frac{du_{00}}{dy} - \left(M + \frac{1}{K}\right) u_{00} = -G_r \theta_0 - G_m \phi_0 \quad (27)$$

$$\frac{d^2 u_{10}}{dy^2} + \frac{du_{10}}{dy} - \left(M + \frac{1}{K} + \frac{i\omega}{4}\right) u_{10} = -G_r \theta_1 - G_m \phi_1 - A \frac{du_{00}}{dy} \quad (28)$$

First-order equations:

$$\frac{d^2 u_{01}}{dy^2} + \frac{du_{01}}{dy} - \left(M + \frac{1}{K}\right) u_{01} = -\frac{d^3 u_{00}}{dy^3} \quad (29)$$

$$\frac{d^2 u_{11}}{dy^2} + \frac{du_{11}}{dy} - \left(M + \frac{1}{K} + \frac{i\omega}{4}\right) u_{11} = -\frac{d^3 u_{10}}{dy^3} + \frac{i\omega}{4} \frac{d^2 u_{10}}{dy^2} - A \frac{du_{01}}{dy} - A \frac{d^3 u_{00}}{dy^3} \quad (30)$$

The corresponding boundary conditions are

$$y = 0: u_{00} = h \frac{du_{00}}{dy}, u_{01} = h \frac{du_{01}}{dy}, u_{10} = \frac{du_{10}}{dy}, u_{11} = h \frac{du_{11}}{dy}$$

$$y \rightarrow \infty: u_{00} \rightarrow 0, u_{01} \rightarrow 0, u_{10} \rightarrow 0, u_{11} \rightarrow 0 \quad (31)$$

Solutions of Eqs. (20), (21), (23), (24) and (27) to (30) are

$$\theta_0 = e^{-NP_r y} \quad (32)$$

$$\phi_0 = e^{-q_2 y} \quad (33)$$

$$\theta_1 = b_1 e^{-q_1 y} + (1 - b_1) e^{-NP_r y} \quad (34)$$

$$\phi_1 = b_2 e^{-q_3 y} + b_3 e^{-q_2 y} \quad (35)$$

$$u_{00} = b_4 e^{-q_4 y} + b_5 e^{-NP_r y} + b_6 e^{-q_2 y} \quad (36)$$

$$u_{01} = b_7 e^{-q_4 y} + b_8 y e^{-q_4 y} + b_9 e^{-NP_r y} + b_{10} e^{-q_2 y} \quad (37)$$

$$u_{10} = b_{16} e^{-q_5 y} + b_{11} e^{-q_1 y} + b_{12} e^{-NP_r y} + b_{13} e^{-q_2 y} + b_{14} e^{-q_3 y} + b_{15} e^{-q_4 y} \quad (38)$$

$$u_{11} = b_{17} e^{-q_5 y} + b_{18} y e^{-q_5 y} + b_{19} e^{-q_1 y} + b_{20} e^{-NP_r y} + b_{21} e^{-q_2 y} + b_{22} e^{-q_3 y} + b_{23} e^{-q_4 y} + b_{24} y e^{-q_4 y} \quad (39)$$

Equations (18) and (26) yield

$$\theta = \theta_0 + \epsilon e^{i\omega t} \theta_1 \quad (40)$$

$$\phi = \phi_0 + \epsilon e^{i\omega t} \phi_1 \quad (41)$$

$$u = u_{00} + K_1 u_{01} + \epsilon e^{i\omega t} (u_{10} + K_1 u_{11}) \quad (42)$$

The non-dimensional skin-friction coefficient σ_0 at the plate $y=0$ is given by

$$\sigma_0 = u_{00}'(0) + K_1 u_{01}'(0) + \epsilon e^{i\omega t} \{u_{10}'(0) + K_1 u_{11}'(0)\} - \frac{iK_1 \epsilon \omega e^{i\omega t}}{4} \{u_{10}''(0) + K_1 u_{11}''(0)\} + K_1 (1 + \epsilon A e^{i\omega t}) [u_{00}''(0) + K_1 u_{01}''(0) + \epsilon e^{i\omega t} \{u_{10}''(0) + K_1 u_{11}''(0)\}] \quad (43)$$

The non-dimensional form of the rate of heat transfer in the form of Nusselt number N_u is given by,

$$N_u = \left(\frac{\partial T}{\partial y}\right)_{y=0} = (T_0' + \epsilon e^{i\omega t} T_1')_{y=0} \quad (44)$$

The non-dimensional form of the rate of mass transfer at the plate in terms of Sherwood number S_h is given by

$$S_h = \left(\frac{\partial C}{\partial y}\right)_{y=0} = (C_0' + \epsilon e^{i\omega t} C_1')_{y=0} \quad (45)$$

The constants are obtained but not given here due to brevity.

3. DISCUSSION OF THE RESULTS

The purpose of the present study is to find out the visco-elastic effects on transient MHD flow with heat and mass transfer in presence of radiation and chemical reaction of Walters liquid (Model B') past a vertical plate in a porous medium. The visco-elastic effect is characterized by the non zero values of the non dimensional parameter K_1 whereas $K_1=0$ represents the Newtonian fluid flow phenomenon.

All the numerical calculations are to be carried out for $P_r=3, G_r=5, G_m=5, h=1, K=1, \epsilon=0.001, \omega=1, \omega t=\pi/2$ throughout the problem.

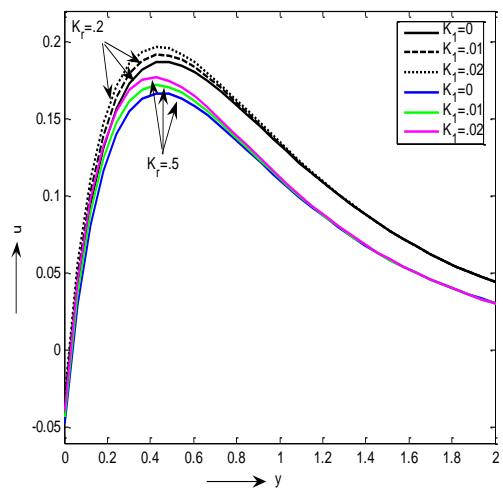


Fig.1. Fluid velocity u against y for R=.2, M=1, A=.5, S_c=.1

Figure 1 illustrates that the fluid velocity u enhances with the growth of the visco-elastic parameter K_1 and diminishes with the rise of chemical reaction parameter K_r . It has also been noticed that the magnitude of the velocity profile against y first increases up to a certain value and then begins to diminish till it becomes zero at large distance from the plate $y=0$ for both non-Newtonian and Newtonian fluid flows.

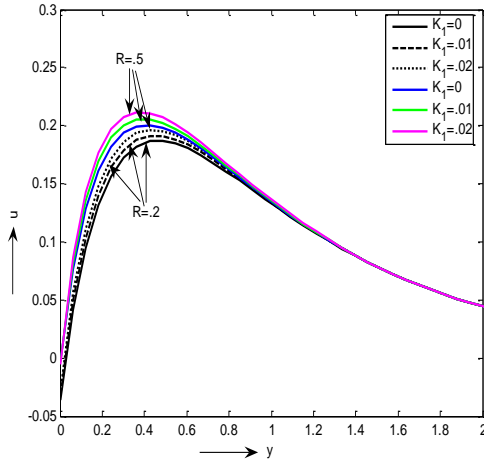


Fig. 2. Fluid velocity u against y for $K_r=2$, $M=1$, $A=5$, $S_c=1$

Figure 2 describes that the fluid velocity u has an accelerating trend with the rising effect of the visco-elastic parameter K_1 and the radiation parameter R as well. It is also observed that the magnitude of the fluid velocity against y first increases up to a certain value and then begins to diminish till it becomes zero at large distance from the plate $y=0$ for both non-Newtonian and Newtonian fluid flows.

Figures 3, 4 and 5 illustrate the behavior of skin-friction coefficient σ_0 at the plate $y=0$ against the suction parameter A , the magnetic parameter M and the Schmidt number S_c respectively.

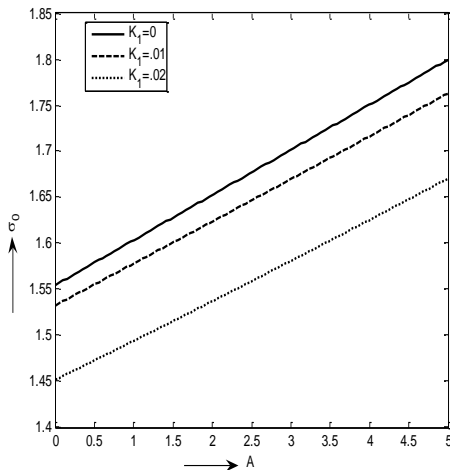
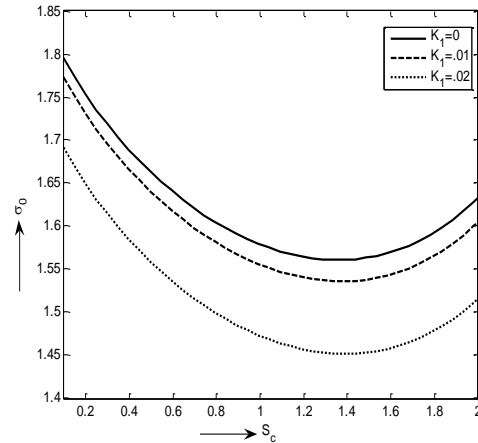


Fig.3. Skin friction coefficient σ_0 against A on the plate $y=0$ for $R=2$, $K_r=2$, $M=1$, $S_c=1$

Figure.3 illustrates that the skin friction coefficient σ_0 at the plate $y=0$ against the suction parameter A



diminishes with the growing effect of the visco-elastic parameter K_1 but enhances with the increase of A .

Figure. 4 depicts that the skin friction coefficient σ_0 at the plate $y=0$ against the magnetic parameter M diminishes with the rising effect of both the visco-elastic parameter K_1 and the magnetic parameter M .

Fig.4. Skin friction coefficient σ_0 against M on the plate $y=0$ for $R=2$, $K_r=2$, $A=5$, $S_c=1$

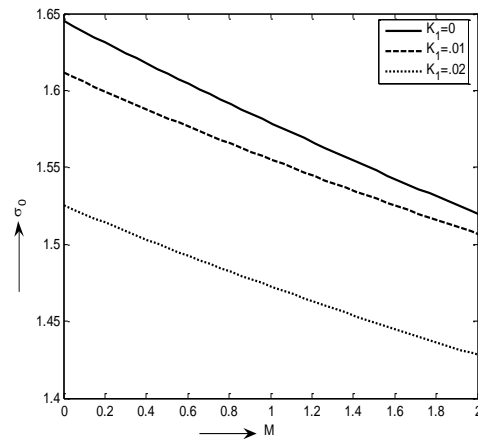


Fig.5. Skin friction coefficient σ_0 against S_c on the plate $y=0$ for $R=2$, $K_r=2$, $A=5$, $M=1$

Figure.5 exhibits that the skin friction coefficient σ_0 at the plate $y=0$ against the Schmidt number S_c diminishes with the growth of the visco-elastic parameter K_1 . It is also found that the magnitude of the skin-friction coefficient at the plate $y=0$ against the Schmidt number S_c first decreases up to a certain value of S_c and then increases in the interval (.1, 2).

4. CONCLUSION

An analysis of free convective transient flow of a visco-elastic fluid characterized by Walters liquid (Model B) over a vertical porous plate through porous media in presence of radiation and chemical

reaction with heat and mass transfer is presented when a transverse uniform magnetic field normal to the plate and a transverse variable suction velocity are applied on the porous plate for different values of visco-elastic parameter K_1 in combination of other flow parameters.

This study leads to the following conclusions:

- ❖ The velocity field is considerably affected by the visco-elastic parameter along with other flow parameters.
- ❖ The velocity field has an accelerating trend with the growing effect of the visco-elastic parameter.
- ❖ The velocity field exhibits an increasing trend with the enhancement of the radiation parameter.
- ❖ The velocity field diminishes with the rise of the chemical reaction parameter.
- ❖ The skin friction coefficient shows a decelerating trend with the rise of the visco-elastic parameter against all of suction parameter, magnetic parameter and Schmidt number.
- ❖ decelerating trend with the rise of the visco-elastic parameter against all of suction parameter, magnetic parameter and Schmidt number.

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