Characteristics of Homogeneous-Heterogeneous Reactions and Melting Heat Transfer in the Stagnation Point flow of Jeffrey Fluid

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ABSTRACT

This work focuses on melting heat transfer in the stagnation point flow of Jeffrey fluid past an impermeable stretching cylinder with homogeneous-heterogeneous reactions. Characteristics of magnetohydrodynamic flow are explored in presence of heat generation/absorption. Diffusion coefficients of species A and B are taken of the same size. Heat released during chemical reaction is negligible. A system of ordinary differential equations is obtained by using suitable transformations. Convergent series solutions are derived. Impacts of various pertinent parameters on the velocity, temperature and concentration distributions are discussed. Numerical values of skin friction coefficient and Nusselt number are computed and analyzed. Present results are compared with the previous published data.

Keywords: Stagnation point flow; Melting heat transfer; Homogeneous-Heterogeneous reactions; Jeffrey fluid.

1. INTRODUCTION

Scientists and researchers are still interested in exploring the behaviors and characteristics of non-Newtonian fluids. Such inspiration is due to numerous applications of non-Newtonian fluids in physiology, pharmaceuticals, fiber technology, coating of wires, food products, crystal growth etc. Characteristics of non-Newtonian fluids cannot be analyzed by a single constitutive relationship. Therefore various models are proposed for the non-Newtonian fluids. Generally the non-Newtonian fluids are categorized into three main types i.e., (i) Differential type (ii) Rate type and (iii) Integral type. Rate type fluids describe the behavior of relaxation and retardation times. Maxwell fluid is a subclass of rate type material which exhibits the behavior of relaxation time only. This model does not present the behavior of retardation time. Thus Jeffrey fluid model (Turkyilmazoglu and Pop (2013), Hayat et al. (2015), Ellahi et al. (2014), Dalir et al. (2015), Hayat et al. (2013)) is proposed to fill this void. Jeffrey fluid model characterizes the linear viscoelastic properties of fluids which has wide spread applications in the polymer industries.

Recently the phenomenon of melting heat transfer has received the attention of researchers and scientists due to their widespread applications in the advanced technological and industrial processes. The melting of soil, the freezing of soil around the heat exchanger coils of a ground based pump, melting of permafrost, magma solidification, thawing of frozen grounds, the freeze treatment of sewage, the preparation of semiconductor material, the casting and welding of a manufacturing process are the important applications of melting phenomenon (Rahman et al. (2013)). Robert (1985) for the first time described melting phenomenon of ice slab placed in a hot stream of air. Hayat et al. (2013) presented boundary layer stagnation point flow of melting heat transfer in Powell-Eyring fluid. Radiative melting heat transfer in the magnetohydrodynamic flow over a moving surface was investigated by Das (2014). Characteristics of melting heat transfer in the flow of Maxwell fluid with double diffusive convection were explored by Hayat et al. (2014). Awais et al. (2014) examined melting heat transfer in the boundary layer stagnation point flow of Burgers' fluid. Prasad et al. (2014) analyzed melting heat transfer and mixed convection boundary layer flow of non-Newtonian fluid saturated by porous medium over a vertical plate.

Chemical reactions in the natural processes involve
both homogeneous and heterogeneous reactions. Also there exist some of the reactions which have less ability to proceed quickly or not at all, except in the presence of a catalyst. The interaction between the homogeneous and heterogeneous reactions are very complex involving the production and consumption of reactant species at different rates both within the fluid and on the catalyst surface such as reactions occurring in combustion, catalysis and biochemical systems. Merkin (1996) explored the properties of homogeneous-heterogeneous reactions in the boundary layer flow for isothermal model. Characteristics of homogeneous-heterogeneous reactions in micropolar fluid embedded in porous medium past a stretching/shrinking sheet were analyzed by Shaw et al. (2013). The analysis of homogeneous-heterogeneous reactions in flow of nanofluid past a permeable stretching sheet was examined by Kameswaran et al. (2013).

The objective of the present investigations is to explore the characteristics of homogeneous heterogeneous reactions in the stagnation point flow of Jeffrey fluid past a cylinder with melting heat transfer. Behavior of heat transfer is modeled and analyzed with heat generation/absorption. Diffusion coefficients of both species are assumed equal. Convergent series solutions are computed via homotopy analysis method (Liao (2012), Turkyilmazoglu (2012), Beg et al. (2012), Shehradz et al. (2014), Abbasbandy (2013), Hayat et al. (2015)). Behavior of various pertinent parameters on the skin friction coefficient and Nusselt number are presented numerically. Present results for skin friction coefficient and Nusselt number are compared with previous published work in limiting sense. Excellent agreement between the results is obtained.

2. Mathematical Formulation

We consider the steady melting heat transfer in the stagnation point flow of Jeffrey fluid by an impermeable stretching cylinder. Magneto-hydrodynamic flow analysis is explored with homogeneous-heterogeneous reactions and heat generation/absorption. Cylindrical coordinates are chosen in such a way that $\chi$-axis is along the axial direction of cylinder while $r$-axis is normal to it. Stretching velocity of the cylinder is originated by applying two forces which are equal in magnitude but opposite in direction such that origin is kept fixed. Ambient temperature $T_m$ is assumed greater than the melting surface temperature $T_m$. The heat released by the reaction is assumed negligible. The homogeneous reaction for cubic autocatalysis can be expressed as follows:

$$ A + 2B \rightarrow 3B, \quad \text{rate} = k_{ab}b^2. \quad (1) $$

while first-order isothermal reaction on the catalyst surface is presented in the form

$$ A \rightarrow B, \quad \text{rate} = k_a a. \quad (2) $$

Here $a$ and $b$ are the concentrations of chemical species $A$ and $B$ while $k_1$ and $k_2$ are the rate constants. These equations of reactions ensure that the reaction rate is zero in the external flow and at the outer edge of the boundary layer. Using the boundary layer approximations ($o(x) = o(u) = o(1)$, $o(r) = o(\nu) = o(\delta)$), the conservation laws of mass, linear momentum and energy take the forms:

$$ \frac{\partial (r v)}{\partial r} + \frac{\partial (r u)}{\partial x} = 0, \quad (3) $$

$$ \frac{\partial u}{\partial x} + \frac{\partial v}{\partial r} = \frac{U e}{r} \frac{dU_k}{dx} + \frac{v}{1 + \lambda_1} \left( \frac{\partial^2 u}{\partial r^2} + \frac{2}{r} \frac{\partial u}{\partial r} + \frac{\partial^2 u}{\partial \chi^2} \right) $$

$$ \left( \frac{1}{r} \frac{\partial u}{\partial r} + \frac{1}{r^2} \frac{\partial^2 u}{\partial \chi^2} \right) + \lambda_2 \left( \frac{v^2 u}{r} + \frac{\partial u}{\partial r} \frac{\partial^2 u}{\partial \chi^2} + \frac{\partial u}{\partial \chi} \frac{\partial^2 u}{\partial r \partial \chi} + \frac{\partial^3 u}{\partial \chi^3} \right) $$

$$ - \frac{\sigma B_0^2}{\rho} (u - U_e), \quad (4) $$

$$ \frac{\partial T}{\partial x} + \frac{\partial v}{\partial r} = \frac{k}{\rho c_p} \left( \frac{\partial^2 T}{\partial \chi^2} + \frac{1}{r} \frac{\partial T}{\partial r} \right) + \frac{Q_0}{\rho c_p} (T - T_m), \quad (5) $$

with

$$ \frac{\partial u}{\partial x} + \frac{\partial v}{\partial r} = D_A \left( \frac{\partial^2 a}{\partial r^2} + \frac{1}{r} \frac{\partial a}{\partial r} \right) - k_{ab}a^2. \quad (6) $$

$$ \frac{\partial b}{\partial x} + \frac{\partial v}{\partial r} = D_B \left( \frac{\partial^2 b}{\partial r^2} + \frac{1}{r} \frac{\partial b}{\partial r} \right) + k_{ab}b^2. \quad (7) $$

The subjected boundary conditions are

$$ u = U_w(x) = U_0x, \quad T = T_m, \quad D_A \frac{\partial a}{\partial r} = -k_a a \text{ at } r = R, $$

$$ u \rightarrow U_e(x) = \frac{U_e x}{l}, \quad T \rightarrow T_e, \quad a \rightarrow a_0, \quad b \rightarrow 0 \text{ as } r \rightarrow \infty, $$

$$ k (\frac{\partial T}{\partial r})_{r=R} = \rho \left( \lambda_c + c_p (T_m - T_o) \right) v(x, R). \quad (8) $$

In the above expressions $u$ and $v$ denote the velocity components in the axial and radial directions respectively, $\sigma$ is the electrical conductivity, $B_0$ is the magnetic field, $\lambda_1$ is the ratio of relaxation to retardation times, $\lambda_2$ is the retardation time, $R$ is the radius of cylinder, $U_w$ and $U_e$ are the stretching and free stream velocities respectively, $\nu$ is the kinematic viscosity, $k$ is the thermal conductivity, $\rho$ is the density, $c_p$ is the specific heat, $Q_0$ is the heat generation/absorption coefficient, $D_A$ and $D_B$ are diffusion species coefficients of $A$ and $B$, $T$ and $T_m$ are the fluid and
melting surface temperatures, \( T_\infty \) is the ambient fluid temperature, \( \ell \) is the characteristic length, \( a_0 \) is the positive dimensional constant, \( \lambda \) is the latent heat of the fluid, \( T_0 \) and \( c_0 \) are the temperature and heat capacity of the cylinder surface.

Considering the following transformations

\[
\eta = \frac{U_0}{v l} \left( \frac{2 - R^2}{2R} \right), \quad \psi = \sqrt{\frac{U_0 v x R f' (\eta)}},
\]

\[
u = \frac{U_0 x}{l} f' (\eta),
\]

\[
v = - \frac{\sqrt{U_0}}{l} R f (\eta), \quad \theta(\eta) = \frac{T - T_m}{T_\infty - T_m},
\]

\[
g(\eta) = \frac{a}{a_0}, \quad h(\eta) = \frac{b}{a_0},
\]

incompressibility condition is satisfied automatically and Eqs. (4) to (7) are reduced to

\[
(1 + 2 \eta) f'' + \left( 1 + \lambda_1 \right) f' f'' - (f')^2 + 2 \eta f'
\]

\[
+ \eta \beta (f f' - 3 f^2) + (1 + 2 \eta) \beta \left( f'^2 - f'' \right)
\]

\[
+ \left( 1 + \lambda_1 \right) \left( A^2 + Ha A^2 \right) \left( 1 + \lambda_1 \right) Ha A^2 f' = 0,
\]

(10)

\[
(1 + 2 \eta) \theta'' + 2 \eta \theta' + Pr f \theta' + Pr \theta \eta = 0,
\]

(11)

\[
\frac{1}{Sc} \left( (1 + 2 \eta) g'' + 2 \eta g' \right) + f g' - K g h^2 = 0,
\]

(12)

\[
\frac{\delta_1}{Sc} \left( (1 + 2 \eta) h'' + 2 \eta h' \right) + h l + K g h^2 = 0,
\]

(13)

with

\[
f'(0) = 1, \quad \theta(0) = 0, \quad g'(0) = K g(0),
\]

\[
\delta f'(0) = - K g(0),
\]

\[
f'(\infty) \rightarrow \Delta, \quad \theta(x) \rightarrow 1,
\]

\[
g(x) \rightarrow 1, \quad h(x) \rightarrow 0,
\]

(14)

\[
Pr f(0) + M \theta''(0) = 0,
\]

(15)

where \( \gamma \) is the curvature parameter, \( A \) is the ratio of velocities, \( \lambda_1 \) is the ratio of relaxation to retardation times, \( \beta \) is the Deborah number in terms of retardation time, \( Ha \) is the Hartman number, \( Pr \) is the Prandtl number, \( \delta \) is the heat generation/absorption parameter, \( K \) is the strength of homogeneous reaction parameter, \( K_s \) is the strength of heterogeneous reaction parameter, \( \delta_1 \) is the ratio of mass diffusion coefficients, \( Sc \) is the Schmidt number and \( M \) is the melting parameter. These quantities are defined as follows:

\[
\gamma = \left( \frac{v l}{U_0 R^2} \right)^{1/2}, \quad Pr = \frac{\mu \nu p}{k}, \quad \beta = \frac{\lambda_2 U_0}{l},
\]

\[
A = \frac{U_\infty}{U_0}, \quad Sc = \frac{v}{D_a}, \quad K = \frac{k g K g g}{U_w},
\]

\[
\delta_1 = \frac{D_R}{D_1}, \quad K_s = \frac{k_s}{D_1} \frac{v l}{U_0}, \quad M = \frac{e_p (T_0 - T_m)}{\lambda_1 + c_0 (T_0 - T_m)}, \quad \delta = \frac{Q f}{U_0 \omega p_{f}}.
\]

(16)

Here it is assumed that diffusion coefficients of chemical species \( A \) and \( B \) to be of a comparable size. This argument provides us to make further assumption that the diffusion coefficients \( D_A \) and \( D_B \) are equal i.e. \( \delta_1 = 1 \) and thus (Kameswaran et al. (2013)):

\[
g(\eta) + h(\eta) = 1.
\]

(17)

Now Eqs. (12) and (13) yield

\[
\frac{1}{Sc} \left( (1 + 2 \eta) g'' + 2 \eta g' \right) + f g' - K g (1 - g)^2 = 0,
\]

(18)

with the boundary conditions

\[
g'(0) = K_s g(0), \quad g(\eta) \rightarrow 1 \quad \text{as} \quad \eta \rightarrow \infty.
\]

(19)

Skin friction coefficient and local Nusselt number are defined as follows:

\[
C_f = \frac{\tau_w}{\rho \nu^2}, \quad Nu_a = \frac{x d w}{k (T_\infty - T_m)},
\]

\[
\tau_w = \frac{\mu}{1 + \lambda_1} \left[ \left( \frac{\partial u}{\partial r} \right) + \lambda_2 \left[ \frac{\partial^2 u}{\partial r^2} + \frac{u}{\partial r} \frac{\partial^2 u}{\partial \theta^2} \right] \right]_{r=R}.
\]

(20)

\[
q_w = -k \left( \frac{\partial T}{\partial r} \right)_{r=R}.
\]

(21)

Dimensionless skin friction coefficient and local Nusselt number are

\[
C_f Re^{1/2} = \frac{1}{(1 + \lambda_1)} \left[ f'(0) - \beta f(0) f''(0) \right] - \frac{\beta f(0) f'(0)}{+ \beta f'(0) f''(0)}.
\]

(22)

\[
Nu_a Re^{1/2} = -\theta'(0).
\]

(23)

where \( Re = \frac{U_w x}{\nu} \) is the Reynolds number.

3. HOMOTOPIC SOLUTIONS

Homotopy analysis method was first proposed by Liao (2012) in 1992 which is used to obtain the solutions of highly nonlinear problems. It provides us a great freedom to choose the initial guesses and linear operators for the construction of series solutions. Thus we have

\[
f_0(\eta) = A \eta + \left( 1 - A \right) \left( 1 - \exp(-\eta) \right), \quad M = \frac{A}{Pr},
\]

\[
\delta_0(\eta) = 1 - \exp(-\eta),
\]

\[
g_0(\eta) = 1 - \frac{1}{2} \exp(-K_s \eta).
\]

(23)
\[ L_f(f) = \frac{d^3 f}{d\eta^3} - \frac{df}{d\eta}, \quad L_\theta(\theta) = \frac{d^3 \theta}{d\eta^3} - \theta, \]

\[ L_g(g) = \frac{d^2 g}{d\eta^2} - g, \quad (24) \]

with

\[ L_f\left[ A_1 + A_2 \exp(\eta) + A_3 \exp(-\eta) \right] = 0, \quad (25) \]
\[ L_\theta\left[ A_4 \exp(\eta) + A_5 \exp(-\eta) \right] = 0, \quad (26) \]
\[ L_g\left[ A_6 \exp(\eta) + A_7 \exp(-\eta) \right] = 0, \quad (27) \]

where \( A_i \ (i=1,2,\ldots,7) \) are the arbitrary constants.

The zeroth and \( m \)th order deformation problems are:

Convergence analysis

Homotopy analysis technique provides us great freedom and an easy way to adjust and control the convergence region of the series solutions. Convergence region is the region parallel to \( h \) axis. Therefore we have plotted the \( h \) curves in the Figs. 1-2. It is found that the admissible ranges of the auxiliary parameters \( h_f, h_\theta \) and \( h_g \) are \(-1.3 \leq h_f \leq -0.8, \quad -1.2 \leq h_\theta \leq -0.8 \) and \(-1.15 \leq h_g \leq -0.6 \).

4. DISCUSSION

The main focus of this section is to analyze the characteristics of various parameters on the axial velocity, temperature and concentration distributions. Characteristics of ratio parameter \( A \) on the velocity distribution are illustrated in Fig. 3. It is concluded that velocity profile increases for \( A > 1 \) and for \( A < 1 \) the boundary layer thickness has opposite effects. It is also examined that there is no formation of boundary layer for \( A = 1 \) i.e., fluid and cylinder move with the same velocity. Fig. 4 shows the behavior of Deborah number \( \beta \) on the velocity distribution. Here we analyzed that velocity distribution enhances for larger values of Deborah number. Higher values of Deborah number corresponds to higher characteristics of elasticity which is responsible in enhancement of the velocity profile. Influence of melting parameter \( M \) on the velocity distribution is displayed in Fig. 5. It is noted that velocity distribution is higher for larger values of melting parameter. As a result of melting, more heat transfers from the heated fluid to the melting surface which corresponds to higher convection flow. Therefore velocity profile increases. Effect of curvature parameter \( \gamma \) on the velocity profile is sketched in Fig. 6. Velocity profile decreases near the surface of cylinder while it increases gradually far away from the surface.

![Fig. 1. h curve for f.](image1)

![Fig. 2. h curves for \( \theta \) and \( \phi \).](image2)

![Fig. 3. Effect of \( A \) on \( f' \).](image3)

![Fig. 4. Effect of \( \beta \) on \( f' \).](image4)
In fact for higher values of curvature parameter, the radius of cylinder decreases which reduces contact area of the cylinder with the fluid. Therefore velocity profile increases. Characteristics of Prandtl number $Pr$ on temperature distribution is sketched in Fig. 7. It is shown that temperature distribution increases for larger values of Prandtl number. Prandtl number is the ratio of momentum diffusivity to thermal diffusivity. Higher Prandtl number corresponds to lower thermal diffusivity. Hence less heat is transferred from heated fluid to the melting surface and as a result the temperature distribution remains higher. Behavior of melting parameter $M$ on the temperature distribution is shown in Fig. 8. Temperature distribution is higher for small values of melting parameter. Further higher values of melting parameter result in enhancement of thermal boundary layer thickness. It is due to fact that more heat transfers from heated fluid to the melting surface due to higher melting parameter which results in the reduction of temperature distribution. Influence of heat generation/absorption on temperature profile is presented in Fig. 9. Temperature profile decreases with an increase in heat absorption parameter $\delta < 0$ while it increases with an increase in heat generation parameter $\delta > 0$. It is also noted that thermal boundary layer thickness has opposite effects for heat generation and absorption parameters. In case of heat generation more heat produced which is responsible for enhancement of temperature profile. Effect of curvature parameter $\gamma$ on temperature profile is sketched in Fig. 10. It is found that temperature profile increases near the surface of cylinder while it decreases away from the surface. For higher values of curvature parameter, the radius of cylinder decreases which offers less resistance. Therefore temperature near the surface of cylinder increases. Influence of strength of homogeneous reaction $K$ on concentration distribution is sketched in Fig. 11. Concentration profile decreases while boundary layer thickness increases for higher values of strength of homogeneous reaction parameter. Behavior of strength of heterogeneous reaction parameter $K_s$ on the concentration distribution is analyzed in Fig. 12. Concentration distribution decreases near the surface of cylinder and it increases away from the surface for higher values of $K_s$. 

Fig. 5. Effect of $M$ on $f'$. 

Fig. 6. Effect of $\gamma$ on $f'$. 

Fig. 7. Effect of $Pr$ on $\theta$. 

Fig. 8. Effect of $M$ on $\theta$. 

Fig. 9. Effect of $\delta$ on $\theta$. 

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Table 1 shows the convergence analysis of the series solutions for momentum, energy and concentration equations. It is concluded that 21st order of approximations are sufficient for convergence analysis of momentum equation while 25th order of approximations are enough for energy and concentration equations. Table 2 presents behavior of various parameters on skin friction coefficient. Higher values of $\gamma$, $\beta$ and $Ha$ result in enhancement of skin friction coefficient while it decreases for larger values of $A$, $\lambda$, and $M$. Table 3 shows the characteristics of various pertinent parameters on Nusselt number. It is noted that Nusselt number increases for higher values of $\gamma$, $Pr$, $\delta$ and $A$ while it decreases with an increase in $M$ and $Ha$. Tables 4 and 5 represent the comparison of skin friction coefficient and Nusselt number with the previous published work of Awais et al. (2013), Mahapatra and Gupta (2002), Pop et al. (2004) and Sharma and Singh (2009). The results show excellent agreement.

Table 1 Convergence of series solutions for different order of approximations when $\lambda = 1.2$

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<th>$\theta'(0)$</th>
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Table 2 Numerical values of skin friction coefficient for different parameters when $Pr = 1.2$ and $\delta = 0.1$

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<th>$\lambda$</th>
<th>$\gamma$</th>
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5. CLOSING REMARKS

In the presented analysis, we have explored the characteristics of melting heat transfer in the MHD stagnation point flow of Jeffrey fluid induced by an impermeable stretching cylinder with homogeneous-heterogeneous chemical reactions. Heat transfer characteristics are modeled and analyzed with heat generation/absorption. The key points are summarized as follows:

- Melting parameter results in enhancement of velocity and associated boundary layer thickness.
Velocity distribution decreases near the surface of cylinder while it increases away from the surface for higher values of curvature parameter.

Temperature distribution decreases for higher values of melting parameter while thermal boundary layer thickness increases.

Concentration distribution decreases for larger values of strength of homogeneous reaction $K$.

Higher values of strength of heterogeneous reaction $K_s$ result in enhancement of concentration profile.

**Table 3** Numerical values of Nusselt number for different parameters when $\gamma = 1.2$ and $\beta = 0.1$

<table>
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<th>$\gamma$</th>
<th>Pr</th>
<th>$\delta$</th>
<th>$M$</th>
<th>Ha</th>
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**Table 4** Comparison of skin friction coefficient ($f'(0)$) with Mahapatra and Gupta (2002), Pop et al. (2004) and Sharma and Singh (2009) for various values of $A$ when $\gamma = 0, \lambda = 0, \beta = 0$, $Ha = 0$, $\delta = 0$ and $M = 0$

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**ACKNOWLEDGMENT**

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**REFERENCES**


