Aerodynamic Forces Acting on Ahmed-Type Vehicles under Fluctuating Headwind Conditions

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ABSTRACT

Aerodynamic forces of Ahmed-type road vehicles subjected to atmospheric fluctuation were studied in an advanced wind tunnel with programmable settings enabling the generation of pulsating wind speeds. The experiments were performed with a time-averaged airflow speed of approximately 13 m/s, with the fluctuating speed ranging from 2.58 to 2.90 m/s, and periods ranging from 1.5 to 5.0 s. The results of the time-dependent drag and lift forces acting on the vehicle were compared with those under steady wind conditions. Further, the influence of the rear slant angle of the Ahmed model on the forces was addressed. The fluctuation in wind speed showed a greater effect on the aerodynamic forces than predicted. The amplitude of the drag force under the pulsating wind became larger in a vehicle having a shape that experienced a large drag force under steady wind conditions. It is concluded that even under fluctuating wind conditions, there exists a critical angle of 30\textdegree at which the vehicle experiences either high or low fluid forces.

Keywords: Road vehicle; Fluctuating wind; Aerodynamic characteristics; Ahmed body, Wind-tunnel experiment.

1. INTRODUCTION

This study aimed at investigating the aerodynamic characteristics of a vehicle subjected to periodically fluctuating headwinds and clarifying the effect of the rear shape of the vehicle on these characteristics.

In recent years, the emphasis on conservation of the environment and reduction in energy consumption has significantly increased. In the automotive industry, research and development of vehicles with low flow resistance has become prevalent owing to the increased interest in the development of electric vehicles (EVs) (Kaneko, 2016). For this reason, wind-tunnel tests are conducted extensively. The wind tunnels employed in these experiments are becoming larger to test full-scale vehicles (Tadakuma \textit{et al.}, 2015; Kato and Hashizume, 2015). Furthermore, they have evolved in type, from fixed to movable-floor wind tunnels (Takagi, 2012). Thus, wind-tunnel tests are often conducted under conditions close to real on-road conditions (Takagi, 2012; Sumida, 2017). However in most wind-tunnel experiments, measurements are taken at a constant airflow speed. Therefore, when applying the results obtained in such a way to a real driving situation, it is necessary to consider changes in environmental conditions. Thus, flow situations in environmental conditions during real driving are determined beforehand, and a more fundamental investigation is required for the explication of aerodynamic characteristics (Tadakuma \textit{et al.}, 2015).

Hucho and Sovran (1993) reviewed past studies on aerodynamics of road vehicles. In addition, Choi \textit{et al.} (2014) explained recent research trends related to aerodynamic characteristics of large vehicles. In these papers, the importance of investigating the unsteady flow behavior around a vehicle body is advocated strongly. The same is emphasized by Fuller \textit{et al.} (2013). However, the effect of ever-changing environmental conditions on aerodynamic characteristics remains undiscussed. Almost all studies have been conducted under conditions involving a constant driving speed or wind speed.

Nevertheless, as stated above, vehicles are frequently driven in natural wind conditions determined by atmospheric fluctuations. This causes a change in wind direction against the direction of vehicle movement, and the vehicles, in
a sense, may be subjected to a fluctuating headwind. The aerodynamic characteristics under such a fluctuating wind condition are very important, particularly for large vehicles such as buses and trucks. The need for analyzing aerodynamic characteristics under not only conventional steady airflow conditions but also under fluctuating airflow conditions was emphasized by Wordley and Saunders (2008), Fuller et al. (2013), and Liu et al. (2016). When the test is conducted in a natural wind environment, the vehicle is under the influence of uncontrolled atmospheric fluctuations. Consequently, it becomes difficult to reproduce on-road conditions and compare data on natural winds and road conditions. For this reason, systematic studies are difficult to execute, and it seems that such studies have not been conducted yet. If a wind tunnel that can simulate environmental airflow is used, aerodynamic characteristics can be analyzed. Therefore, it will be possible to verify (Kato and Hashizume, 2015; Liu et al., 2016; Wordley and Saunders, 2008; Fuller et al., 2013) the correlation between results obtained under steady winds and in on-road experiments. This approach is widely applied in other areas (such as aircraft systems), with the aim of obtaining a valid aerodynamical model (Lichota et al., 2017).

Sumida (2017) measured the fluid forces acting on a blunt-bodied vehicle (Ahmed et al., 1984) under unsteady upstream flow conditions. In that test, an advanced wind tunnel (Sumida, 2017) that could drive its wind to fluctuate periodically was employed. They found that the fluid forces due to fluctuating winds were different from those at a constant wind speed (Sumida, 2017).

On the basis of the above fundamental findings, this study experimentally investigated the fluid forces acting on a vehicle under periodically fluctuating headwind conditions. In the experiment, we employed the Ahmed-type model (Ahmed et al., 1984) as the test vehicle body. Furthermore, we addressed the problems related to vehicles driven at a constant speed but experiencing periodically fluctuating headwinds. In particular, we focused on the time-dependent fluid forces for the various rear slant angles of the Ahmed-type vehicle model. The measurements of the drag and lift forces acting on the models and pressure distributions on the centerline of the models were obtained. Next, by comparing the obtained results with those under steady wind conditions, we determined the effects of the rear slant angle on the unsteady fluid forces. This work will help understand the effects of atmospheric wind fluctuations on aerodynamic characteristics of vehicles.

2. EXPERIMENTAL SETUP AND METHODS

2.1 Wind Tunnel

The experiments were conducted in the advanced wind tunnel at Kindai University’s Research Institute of Fundamental Technology for the Next Generation (KURING) (Sumida, 2017). The schematic of the wind tunnel, experimental set up, and measurement system are shown in Fig. 1. The latter two components were newly constructed on the basis of the previous study (Sumida, 2017). The contraction ratio of the wind tunnel is 5.4:1, and the nozzle exit has a square cross-section of length 600 mm per side. In accordance with the experiment, the wind tunnel can be selectively set in three ways: as a closed-circuit wind tunnel, semi-open wind tunnel, or a single-circuit wind tunnel. Owing to the ease of executing measurements, we chose the semi-open type with the test section being open.

The periodically fluctuating wind was generated using an axial flow blower consisting of 14 blades and driven by a 45 kW electric motor. The rated air volume and rotational speed are 900 m³/min and 1755 rpm, respectively. Varying wind speeds could be obtained by adjusting the maximum and minimum pitch angles of the rotor blades and setting the interval time of the pitching motion. This setting is programmable.

This study aimed at analyzing specific aerodynamic characteristics under fluctuating headwinds and comparing them with those under steady winds. Therefore, although the wind-tunnel facility in
2.2 Test Vehicle Model

The vehicle model employed in the experiment was the Ahmed-type model (Ahmed et al., 1984), shown in Fig. 2, to compare our results with those hitherto obtained under steady wind conditions (Ahmed et al., 1984; Banga et al., 2015). The test model is a 1/2.5-scale Ahmed model (Ahmed et al., 1984) and is therefore approximately 1/12.5 of a practical vehicle. The dimensions are length \( l = 417.6 \text{ mm} \), width \( b = 155.6 \text{ mm} \), and height \( h = 115.2 \text{ mm} \). The section measuring 76.9 mm in the rear part of the model can be adjusted at a slant angle, \( \theta \), ranging from 0 to 40°.

2.3 Experimental Setup and Measurement Procedures

The measurement system is comprised of three parts for measuring the wind speed, aerodynamic force, and pressure (Fig. 1). The velocity of the airflow issued from the wind-tunnel’s nozzle exit was measured using a hot-wire anemometer and Pitot tube. The degree of turbulence at the nozzle exit was less than 0.7% when the wind speed ranged from \( V = 10 \text{ to } 20 \text{ m/s} \). The model was supported by four columns of diameter 8 mm, which were fitted to the multicomponent load cell (Nissho-Electric-Works Co.: LMC-3502). The installation height \( H \) of the model could be changed in the range of 15 to 40 mm. Thereby, the drag, lift, and side components \( (D, L, \text{ and } S, \text{ respectively}) \) of the resultant fluid force \( F \) acting on the vehicle model could be detected. The pressure distribution on the centerline of the vehicle was measured using a differential pressure transducer (JTEKT: DD101K) as shown in Fig. 1. Measurement holes of diameter 1.5 mm were installed around the model at 40 positions or more. The reference pressure \( p_0 \) is the static pressure measured by a Pitot tube located on the top left of the model in the free stream flow, as shown in Fig. 1.

The output voltages of the load cell and pressure transducer were suitably amplified using direct current amplifiers (Nissho-Electric-Works Co.: DSA-100A, and JTEKT: AA3004, respectively). Next, they were converted into digital values through a data acquisition system (Keyence: NR-500), being recorded in a personal computer. At the same time, the time marker signal indicating the position of the pitch angle of the rotor blade was also recorded, as shown in Fig. 1. Data were recorded for approximately 20 fluctuation cycles and sampled for approximately 30 to 120 s.

Data acquisition accuracy was taken into account for measurements of unsteady fluid forces and pressures. The parallelism setting of the model with respect to the flow issued from the nozzle exit was checked by measuring the side force in the steady flow. The side force \( S \) was 1.3% of the drag force \( D \) or less. It was estimated that the accuracy of flow angle of the model was within 0.2°. The errors in the flow angle showed that errors in the free-stream dynamic pressure are 1%, at the most, in the pressure measured. The accuracies of the instruments measuring force and pressure were less than 0.2 and 0.4%, respectively, with respect to their full-scale values. Moreover, the characteristic frequencies of the multicomponent load cell were 170 Hz in the wind direction and 130 Hz in the vertical and lateral directions. The pressure transducers had a characteristic frequency of not less than 3 kHz. The frequency response characteristics were very high compared to an effectuated cycle of 1/1.5 Hz of a pulsating wind.

The data acquisition system was calibrated, as necessary, before the experiments and used. In addition, when the measurements were made, the outputs from the instruments were passed through a low-pass filter of 20 Hz.

2.4 Experimental Conditions

The experiments were mostly carried out at a time-averaged wind speed of \( V_a = 13.0 \pm 0.15 \text{ m/s} \), as mentioned in Table 1. Here, the subscripts \( tu \) and \( os \) indicate time-mean and amplitude values, respectively. These conditions were chosen on the basis of the previous work (Sumida, 2017). The wind configuration is shown in Fig. 3. This speed
Table 1 Experimental conditions in pulsating wind

<table>
<thead>
<tr>
<th>Fluctuation period</th>
<th>Time-averaged wind speed</th>
<th>Fluctuation wind speed</th>
<th>Amplitude ratio $\eta = V_{os}/V_{ta}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$T_s$</td>
<td>$V_{ta} \pm 0.15$ m/s</td>
<td>$V_{os} \pm 0.06$ m/s</td>
<td></td>
</tr>
<tr>
<td>1.5</td>
<td>13.0</td>
<td>2.63</td>
<td>0.202</td>
</tr>
<tr>
<td>2.0</td>
<td>13.1</td>
<td>2.58</td>
<td>0.197</td>
</tr>
<tr>
<td>3.0</td>
<td>12.6</td>
<td>2.90</td>
<td>0.230</td>
</tr>
<tr>
<td>5.0</td>
<td>14.2</td>
<td>2.40</td>
<td>0.169</td>
</tr>
</tbody>
</table>

gives the value of Reynolds number, $Re$, as $3.59 \times 10^6$, where $Re = V_{ta} \rho \ell / \nu$, and $\nu$ is the kinetic viscosity of the air. The conditions are given in the table: $T = 1.5–5.0$ s for the fluctuation period and $V_{os} = (2.40–2.90) \pm 0.06$ m/s for the velocity fluctuation, given the amplitude ratio $\eta = V_{os}/V_{ta} \approx 0.169–0.230$.

3. RESULTS AND DISCUSSION

In the wind-tunnel test using a vehicle model, it is necessary to prior examine the effects of parameters such as the blockage ratio and height from the ground plane on the results (Flow Technology Expert Committee, Wind-Tunnel Correlation Working Group, 1998; Hucho and Sovran, 1993). The blockage ratio in the experiment was less than 1/20 at which there was no effect of the blockage ratio (Hucho and Sovran, 1993; Society of Automotive Engineers of Japan Editorial Board, 2004). The thickness of the boundary layer (Wang et al., 2006) was approximately 8 mm at 285 mm measured from the leading edge of the ground plane, at which the vehicle model is placed, at a free airflow velocity of 13 m/s.

3.1 Fluid Forces in Wind with no Fluctuation and Preliminary Examination

The fluid forces acting on the vehicles were decomposed into the drag and lift forces, $D$ and $L$, respectively. Both components were normalized using the dynamic pressure $\rho V^2/2$ and projected frontal area $A$ of the vehicle model per the following equation, with $\rho$ being the air density.

\[
C_D = \frac{D}{(\rho V^2/2)A}, \quad C_L = \frac{L}{(\rho V^2/2)A}.
\] (1)

Thus, the fluid forces were evaluated using the non-dimensional coefficients of $C_D$ and $C_L$.

3.1.1 Preliminary Measurements

The flow field around the vehicle model is slightly dependent on the structure of the testing part of the wind tunnel (Hausmann et al., 1988; Wickern, 2007). This influences the aerodynamic performance. We performed a preliminary analysis on the influences of the ground-plane length and supporting-column height on the aerodynamic forces acting on the vehicle models.

For the former, it was confirmed that there is no influence of the ground-plane length, $x_0$, measured from the model’s rear end, on the fluid force when $x_0$ is larger than 600 mm, i.e., $x_0/\ell > 1.4$. Thereafter, we performed the experiments with a length $x_0$ of approximately 1200 mm.

Subsequently, the influence of the supporting columns on the fluid forces in the model was examined. The drag force of the columns increased in proportion to the installation height $H$ of the model, and the coefficient of the columns increased slightly with an increase in the wind speed $V$. On the other hand, the drag coefficient $C_D$ of the model gradually decreased as $V$ increased. However, when the wind speed $V$ exceeded 10 m/s, the dependency of the coefficients on $V$ cannot be seen gradually. For $H = 40$ mm, the drag force of the columns corresponded to approximately 15–18% of that of the model, when $V = 10–20$ m/s. On the other hand, the lift force of only the supporting columns was very small compared to that of the model, and the value remained unchanged for a height $H$ of 20–40 mm. Therefore, the corresponding illustrations are omitted.

In wind-tunnel tests (Minguez et al., 2008; Meile et al., 2011; Wang et al., 2013; Banga et al., 2015; Volpe et al., 2015; Keogh et al., 2016; Thacker et al., 2013) and a water-channel test (Tunay et al., 2013) previously conducted with Ahmed-type vehicle models, measurements were obtained at $H = 0.174H$, with a set up geometrically similar to that in the experiment conducted by Ahmed et al. (1984). However, the problem regarding the formation of a boundary layer on the ground plane and its effect on the fluid forces have not been discussed concretely in these works. Therefore, we executed our experiments at $H = 40$ mm ($= 0.347h$) to minimize the influence of the boundary layer formed on the ground plane.

3.1.2 Fluid Forces under Steady Wind

Drag and Lift Coefficients, $C_D$ and $C_L$

Figures 4 and 5 show the relationship between $C_D$ and $C_L$, respectively, and the rear slant angle $\theta$ of the model when $V = 13$ m/s ($Re = 3.59 \times 10^7$). The results show that the dependency of $C_D$ and $C_L$ on $\theta$ is similar to those experimentally found at $Re = 4.29 \times 10^6$ by Ahmed et al. (1984) and numerically obtained at $Re = 1.04 \times 10^7$ by Banga et al. (2015). However, in the latter, the angle of 30° or less is the object of comparison.
That is, although the drag coefficient \( C_D \) takes a lower value at \( \theta = 10^\circ \), it increases rapidly when \( \theta \) becomes larger than 20\(^\circ\), reaching the maximum value at \( \theta = 30^\circ \) (Fig. 4). However, when \( \theta \) remains the same (30\(^\circ\)), the value of \( C_D \) decreases and takes a different lower value. Once the flow is in a state with a high or a low value, the transition to the other state happens rarely. The transition to the state with a high value from the state with a low value, in a general sense, seems to readily occur in terms of percentage.

On the other hand, the lift coefficient \( C_L \) increases as \( \theta \) increases, and at \( \theta = 30^\circ \), it simply takes a high or a low value in accordance with the value of \( C_D \), as shown in Fig. 5. However, when \( \theta \) exceeds 30\(^\circ\), \( C_L \) takes a low value close to the case of \( \theta = 0^\circ \), and the change in \( C_L \) with \( \theta \) becomes small. The reason is as follows. For the case of \( \theta > 30^\circ \), the slant angle steepens, and the vehicle resembles the rear shape at \( \theta = 0^\circ \). Therefore, it appears that the vehicles with \( \theta = 0^\circ \) and \( \theta > 30^\circ \) are subjected to fluid forces owing to a similar flow state.

Although Banga et al. (2015) performed a computational fluid dynamics (CFD) analysis of the vehicles with \( \theta = 0-40^\circ \); however, the values of \( C_D \) and \( C_L \) for slant angles larger than the critical angle were not calculated. According to them, it is because beyond 30\(^\circ\), flow separation occurs, and \( C_D \) and \( C_L \) become randomly dispersed.

**Transition of Fluid Forces for Model with \( \theta = 30^\circ \)**

As has been noted, the fluid force acting on Ahmed-type vehicles drastically changes at a slant angle 30\(^\circ\), which is the critical angle. This paper briefly gives additional explanations. Recently, such a flow was extensively examined for two typical cases of \( \theta = 25^\circ \) and \( \theta = 35^\circ \), with a high and a low force, respectively. There are many works, namely Tunay et al. (2013), Minguez et al. (2008), Aljure et al. (2014), Lehmkuhl et al. (2012), Venning et al. (2015) for \( \theta = 25^\circ \), and Banga et al. (2015) and Wang et al. (2013) for \( \theta = 35^\circ \). In these studies, flow fields around the vehicle were investigated using particle image velocimetry (PIV) (Wang et al., 2013; Venning et al., 2015; Volpe et al., 2015; Thacker et al., 2013; Tunay et al., 2013) and CFD techniques (Banga et al., 2015; Meile et al., 2011; Minguez et al., 2008; Aljure et al., 2014; Lehmkuhl et al., 2012; Tunay et al., 2013). However, their works only provide results obtained for a specific value of \( \theta \). Therefore, a clear explanation concerning the transition mechanism is not available (Banga et al., 2015; Wang et al., 2013; Thacker et al., 2013). This problem remains unsolved.

Considering these situations, we examined how a disturbance locally induced by a circular cylinder affected the occurrence of the transition in fluid forces. Circular cylinders with diameters \( d \) of 8, 12, and 15 mm were installed at a position 287 mm from the tip of the model, as shown in Fig. 6. For example, the transition phenomenon for \( d = 8 \) mm occurred at \( h_c = \pm h/2 \). Furthermore, when the diameter of the cylinder was 12 mm, the transition occurred only at \( h_c = +h/2 \). Fluid forces for \( h_c = 0 \) and \( -h/2 \) took only the high and low value, respectively. Although the results are interesting, we are unable to explain the reasons for these results at this point.

![Fig. 4. Relationship between drag coefficient \( C_D \) and rear slant angle \( \theta \) under steady wind conditions (V= 13 m/s).](image)

![Fig. 5. Relationship between lift coefficient \( C_L \) and rear slant angle \( \theta \) under steady wind conditions (V= 13 m/s).](image)

![Fig. 6. Setup for examination of disturbance induced by a circular cylinder on fluid force transition.](image)
3.2 Fluid Forces under Fluctuating Headwind

In this study, we addressed the flow problem in which a vehicle is running at a fixed speed under wind fluctuations occurring alternately in the traveling and adverse directions, as demonstrated in Fig. 3. That is, the fluctuating wind that a running vehicle receives from the front (headwind) is modeled as a pulsating wind in a wind-tunnel test. Such a fluctuating headwind is expressed in terms of the fluctuation speed and period of fluctuation. Moreover, it is considered that effects of the fluctuation on the aerodynamic force will differ according to the speed of the running vehicle. Therefore, it can be said that the aerodynamic force characteristics of the vehicle, subjected to pulsating winds, depend roughly on the amplitude ratio of the fluctuating wind speed to the speed of the traveling vehicle (time-averaged wind speed) and on fluctuation period. Nevertheless, it is not easy to perform tests under these wind conditions.

3.2.1 Influence of Fluctuation Frequency on Fluid Forces

First, we will discuss the effects of the fluctuation period on the aerodynamic forces. Figure 7 shows changes in the drag and lift forces with time for the model with \( \theta = 20^\circ \) under several fluctuation periods, for which the experimental conditions are mentioned in Table 1. The relationships between the fluid forces and wind velocity for a cycle are illustrated in Fig. 7, in the form of a Lissajous diagram. Here, the wind velocity changes almost sinusoidally with time \( t \) as illustrated later (see Fig. 8). For a fluctuation period \( T = 5 \text{ s} \), there is little difference in the fluid forces of \( D \) and \( L \) in the increasing and decreasing phases of the wind velocity. The change in these forces with time is not quasi-steady even at \( T = 5 \text{ s} \). Moreover, for a fluctuation period of \( 3 \text{ s} \) or less, the influence of the fluctuation of the wind becomes remarkable. For instance, even if the instantaneous wind velocity is the same in a cycle, the airflow causes stronger forces at the increasing phase compared to those at the decreasing phase.

Thus, in this paper, we describe the results obtained for fluctuation period of \( T = 1.5 \text{ s} \), at which the wind fluctuation has the strongest influence on the aerodynamic forces. Now, we will discuss the effect of the slant angle \( \theta \) on the fluid forces.

3.2.2 Influence of Slant Angle on Fluid Forces

Figure 8 shows the results obtained for models with different slant angles under pulsating winds. The time mean and amplitude of the wind velocity are \( V_{\text{av}} = 13.0 \pm 0.15 \text{ m/s} \) and \( V_{\text{os}} = 2.63 \pm 0.06 \text{ m/s} \), respectively, with a pulsation (fluctuation) period of \( T = 1.5 \text{ s} \), as provided in Table 1. This gives the amplitude ratio of \( \eta = V_{\text{os}}/V_{\text{av}} = 0.202 \). In Fig. 8, the changes in \( D \), \( L \), and wind velocity \( V(t) \) with time are illustrated. Here, the abscissa is the phase angle \( \Theta \) which is described later in Eq. (2). The dashed and dotted lines show the time-mean values, and velocity \( V \) is nondimensionalized by the time-averaged value \( V_{\text{av}} \). It can be seen from Fig. 8 that the wind velocity changes almost sinusoidally with time \( t \) and can be simply expressed using the following equation:

\[
V(\Theta) \approx V_{\text{av}} + V_{\text{os}} \cdot \sin \Theta.
\]  

where \( \Theta = \omega t \) is the phase angle and \( \omega \) is the pulsation frequency.

The time-averaged drag force \( D_{\text{av}} \) in each model is slightly larger than the drag force under a steady wind with the same value as the time-averaged velocity of the pulsating wind. The details are described later. Moreover, the fluctuating component of the drag force, \( D_{\text{os}} \), is more than 40% of the time-averaged value \( D_{\text{av}} \), though the amplitude ratio \( \eta \) is 0.202. Furthermore, the drag force varies with a phase lead from the wind fluctuation. The higher the drag force on the model under steady wind conditions, the larger is the phase difference \( \phi_0 \) between \( D \) and \( V \) under pulsating wind conditions. When the slant angle exceeds \( 20^\circ \), the phase difference \( \phi_0 \) reaches \( 16^\circ \). In particular, it is a noteworthy result, shown in Fig. 8(c); both high and low fluid forces evidently occur when the slant angle is \( 30^\circ \), the critical angle under steady wind conditions. At a slant angle of \( 30^\circ \), the model experiences the transition phenomenon of fluid forces even when the wind has not only a local turbulence but also a fluctuation of \( \eta = 0.202 \). The
transition phenomenon appears to depend on the state of starting operation of the wind tunnel for the pulsating wind. For this reason, the transition did not appear while measuring the forces. This issue is arousing the interest of specialized scholars: there appears a transition phenomenon even in an upstream flow with a fluctuation of $\eta = 0.202$. This should be noted while actually driving on the road. On the other hand, the change in the lift force $L$ with time against the wind fluctuation differs considerably while depending on the slant angle. In Fig. 8(a), for a model with symmetric upper and lower halves at $\theta = 0^\circ$, the lift force changes in the opposite phase of the fluctuating wind. In this model, the lift force shows negative values through a cycle because the pressure decrease on the floor side is larger than that on the roof side. Conversely, in models with a slant rear shape, the pressure on the slant surface decreases as the slant angle increases (refer to Fig. 9), causing the lift force to increase in the upward direction (positive values). As a result, the lift force changes in proportion with the increase and decrease in the wind velocity. At a critical angle of $30^\circ$, the lift force takes either a high or low value in accordance with the value of the drag force [Fig. 8(c)]. For the low value, the amplitude of $L$ becomes smaller compared to the cases of other slant angles. In addition, for models with $\theta > 30^\circ$, the fluctuations of $L$ are noticeably small [Fig. 8(d)]. The amplitude ratio of the lift force, $L_{\text{High}}/L_{\text{Low}}$, exceeds 0.4, as calculated from Figs. 8(a) and (b), except when the drag force at $\theta = 30^\circ$ takes a low value. The drag and lift forces act on the vehicles at two or more times the amplitude ratio of the wind speed. Therefore, the fluctuation of the wind speed has a higher effect on vehicles than was generally thought.

**Fig. 8.** Changes in drag and lift forces with time under pulsating wind conditions with period $T = 1.5$ s. Dashed and dotted lines denote time-mean values, $D_{\text{mean}}$ and $L_{\text{mean}}$, respectively.
3.2.3 Changes in Static Pressure on Body Surface with Time

Figure 9 shows variations in static pressures at representative positions, which are on the centerline of the model surface, with time. The abscissa is the phase angle $\Theta$. In the figure, the static pressure $p$ is displayed in the form of the pressure coefficient $C_p$, defined by the following expression:

$$C_p = (p - p_o)/(\rho V_a^2/2).$$

(3)

Here, $p_o$ is the reference pressure that is the static pressure in the wind tunnel measured by the Pitot tube (refer to Fig. 1). Moreover, the positions at which the illustrated pressures were measured are concretely indicated in the upper part of the figure.

The drag force varies principally owing to the change in the pressure on the front surface. This pressure ($F_D$) varies periodically with a phase lead of approximately $15^\circ$ from the wind fluctuation. The pressure coefficient $C_p$ at $F_D$ is in the range of 1.52 to 0.66 and rises rapidly when the headwind becomes strong. The drop in pressure on the nose part of the front ($F_1$ and $F_{11}$) varies with a slight phase delay from the wind fluctuation. The pressure drop in the nose part is slightly large at the floor side ($F_{11}$) compared to that at the roof side ($F_1$). In addition, although $C_p$ on the floor and roof sides takes negative values, the absolute value of the former ($C_{p_1}$) is slightly larger than that of the latter ($C_{p_{11}}$), which is not illustrated in Fig. 9. On the other hand, $C_p$ on the rear surface changes in the opposite phase to that on the front surface, and it takes values ranging from $-0.1$ to $-0.5$. Further, the negative pressure on the slant surface increases with an increase in $\theta$, and it reaches the maximum at $\theta = 30^\circ$. This causes an increase in the drag and lift forces, particularly for the case of $\theta > 20^\circ$. However, when $\theta$ exceeds $30^\circ$, the pressure at $R_1$ is analogous to that at $R_6$ with $\theta = 0^\circ$.

3.2.4 Influence of Slant Angle on Time-Averaged Fluid Forces

Henceforth, we express the fluid forces as dimensionless quantities, and move forward with the examination. The drag and lift forces, $D$ and $L$, were normalized using the dynamic pressure, $\rho V_a^2/2$, and the time-averaged velocity, $V_{in}$, of the wind. They are expressed in the same manner as Eq. (1):

$$C_D(t) = D(t)/(\rho V_{in}^2 A/2),$$
$$C_L(t) = L(t)/(\rho V_{in}^2 A/2).$$

(4)

First, we compared the time-mean values of the drag and lift forces, $C_{D,ta}$ and $C_{L,ta}$, respectively, with the values under steady wind conditions. The results for $C_{D,ta}$ and $C_{L,ta}$ are shown in Figs. 10 and 11, respectively. The time-averaged drag coefficients $C_{D,ta}$ at every slant angle are slightly higher by approximately 3 to 7% compared to those under steady wind conditions (Fig. 10). Accordingly, the power loss corresponding to the increment of the fluid force appears when vehicles are subjected to a fluctuating headwind.

On the other hand, for the lift coefficient, there is a discernible difference in terms of the slant angle, as shown in Fig. 11. The degree of increase in $C_{L,ta}$ due to wind fluctuation is considerably high for models with $\theta \geq 30^\circ$, which take a low resistance. Furthermore, it seems that the lift force is more sensitive than the drag force to wind fluctuations.
3.2.5 Lissajous Diagrams of $C_D$ and $C_L$

Next, we discuss the fluid forces arising from the wind fluctuation in more detail. For this, the relationships between the fluid forces and wind velocity for a cycle are shown in the form of Lissajous diagrams in Figs. 12 and 13. Moreover, Fig. 14 shows the differences, $C_{D,am}$ and $C_{L,am}$, between the maximum and minimum values of $C_D$ and $C_L$, respectively, during a cycle. In addition, the differences in $C_D$ and $C_L$ values at the time when $(V-V_{ta})$ both in the acceleration and deceleration terms become 0 m/s, are shown in Fig. 15. The differences are denoted by $C_{D,dif}$ and $C_{L,dif}$, respectively. They indicate the degree of the phase difference between the force and wind speed under pulsating wind conditions. That is, an increase in their values shows that the phase lead becomes large. In addition, a negative value indicates that the force changes in the opposite phase to the wind speed, as seen from the results at $\theta = 0^\circ$ in Figs. 13 and 15.

In Figs. 12 and 13, $C_D$ and $C_L$ change with time in a clockwise direction, except for $C_L$ at $\theta = 0^\circ$. $C_D$ increases approximately in proportion to the wind speed when the headwind becomes strong. In contrast, it decreases rapidly for the first half of the phase when the wind weakens. The relationship
between \( C_{D,am} \) and \( \theta \) [Fig. 14(a)] is similar to the relationship of \( C_D \) and \( \theta \) under steady wind conditions (Fig. 4). The value of \( C_{D,am} \) ranges from 0.21 to 0.32, and these values correspond to approximately 80% of the \( C_D \) values under a steady wind. \( C_{D,am} \) is small at \( \theta \approx 10^\circ \) and slightly increases when \( \theta \) approaches the value of 30° [Fig. 15(a)].

However, it takes the lowest value at \( \theta = 30^\circ \) with a low fluid resistance. Predominantly, the value of \( C_{D,am} \) is equivalent to one-third of the \( C_D \) value under a steady wind.

On the other hand, the lift coefficient \( C_L \) differs extremely as the slant angle \( \theta \) changes (Fig. 13). In particular, for the model with \( \theta = 0^\circ \) with symmetry between the upper and lower halves, the lift force acts downward for a cycle, and its magnitude is almost proportional to the increase and decrease in the wind, as shown in Fig. 13. The slant-angle dependency of \( C_{L,am} \) is similar to that of \( C_L \) under a steady wind; further, the value of \( C_{L,am} \) is almost the same as that of \( C_L \) under a steady wind [Fig. 14(b)]. Nevertheless, the value of \( C_{D,am} \) is the largest for the model with \( \theta = 20^\circ \), whereas there is little difference for the models with \( \theta \geq 30^\circ \), indicating a low \( C_L \) [Fig. 15(b)].

### 3.2.6 Resultant Force Coefficient and Direction of Its Action

In Fig. 16, the resultant force \( F \) and its direction \( \alpha \) acting on models are shown, in which \( F \) is nondimensionalized in the same manner as Eq. (4), i.e.,

\[
C_r(t) = F(t) / (\rho V_{ta}^2 A) \tag{5}
\]

Here, \( F(t) = (D(t)^2 + L(t)^2)^{1/2} \), and the direction is obtained from \( \alpha = \tan^{-1}[L(t)/D(t)] \).

The \( C_r \) values in the Lissajous diagrams illustrated for each model change clockwise with respect to time, except for \( \alpha \) at \( \theta = 0^\circ \). The resultant force \( F \) for models with \( \theta = 0^\circ \) acts in the direction of \( \alpha \), ranging from \(-20^\circ \) to \(-25^\circ \). It starts to act upward as \( \theta \) increases. \( C_r \) rapidly increases in the range of \( \theta = 12.5 \) to \( 30^\circ \), starting to act in the direction corresponding to approximately \( 44^\circ \). However, when the slant angle exceeds the critical angle of \( 30^\circ \), the direction of \( F \) does not change much with \( \theta \) and time, and \( F \) acts in the direction corresponding to approximately \( 8^\circ \).

### 4. CONCLUSIONS

Wind-tunnel experiments were performed to study the aerodynamics of an Ahmed-body vehicle subjected to fluctuating headwinds. The effects of the slant angle on the fluid forces were investigated. The principal findings are summarized as follows.

1. Unsteady upstream flows exert significant effects on the fluid forces, and the aerodynamic characteristics are dependent on the slant angle of the vehicle’s rear shape. Furthermore, there exist unsteady effects persistently even under a fluctuating wind with a period of period 5 s.

2. The larger the drag force on the model under a steady wind with no fluctuation, the larger is the variation in the drag force during a cycle. The fluctuation of the fluid forces corresponds to approximately twice that of the amplitude ratio of the wind velocity. The time-mean value of the drag force is 3 to 7% higher than that under a steady wind.

3. The difference between the lift forces at the times when the wind speed in the acceleration and deceleration terms becomes equal to the time-averaged speed reaches as much as 40% of the lift force under a steady wind; it is the largest for the model with \( \theta = 20^\circ \).

4. Under a fluctuating wind, the vehicles receive the resultant force, the variation of which corresponds to almost that under a steady wind during a cycle. The force increases in the range of \( \theta = 12.5 \) to \( 30^\circ \), whereas it does not change.
much for $\theta > 30^\circ$.

(5) For models with a slant angle of $30^\circ$, the vehicle experiences either of the high or low fluid forces in the same manner as in the case of a steady wind. The angle corresponds to the critical angle even when the wind shows a large fluctuation.

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